Light Sources I

Takashi TANAKA RIKEN SPring-8 Center

Outline

- Introduction
- Fundamentals of Light and SR
- Overview of SR Light Source
- Characteristics of SR (1)
- Characteristics of SR (2)
- Practical Knowledge on SR

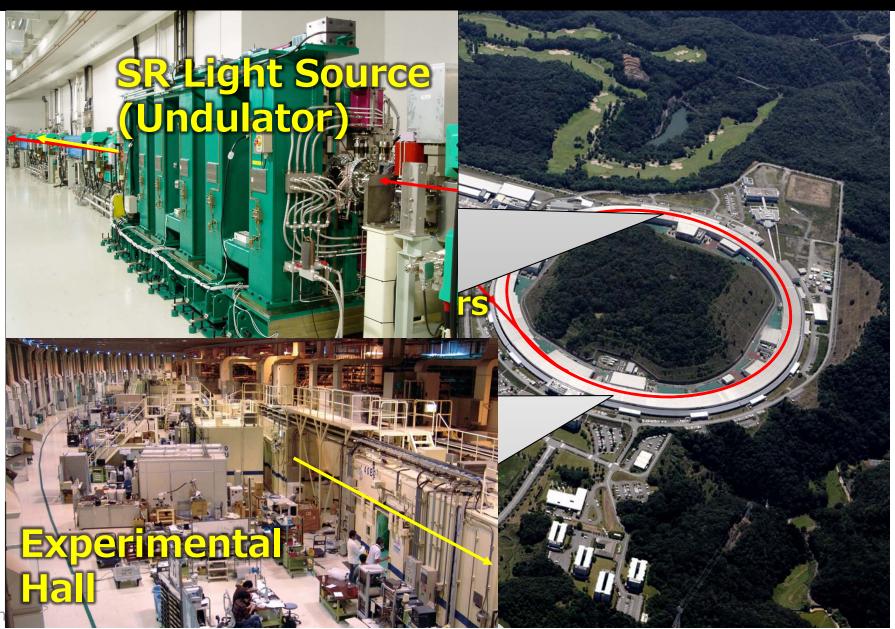
Lecture I?

Lecture II?

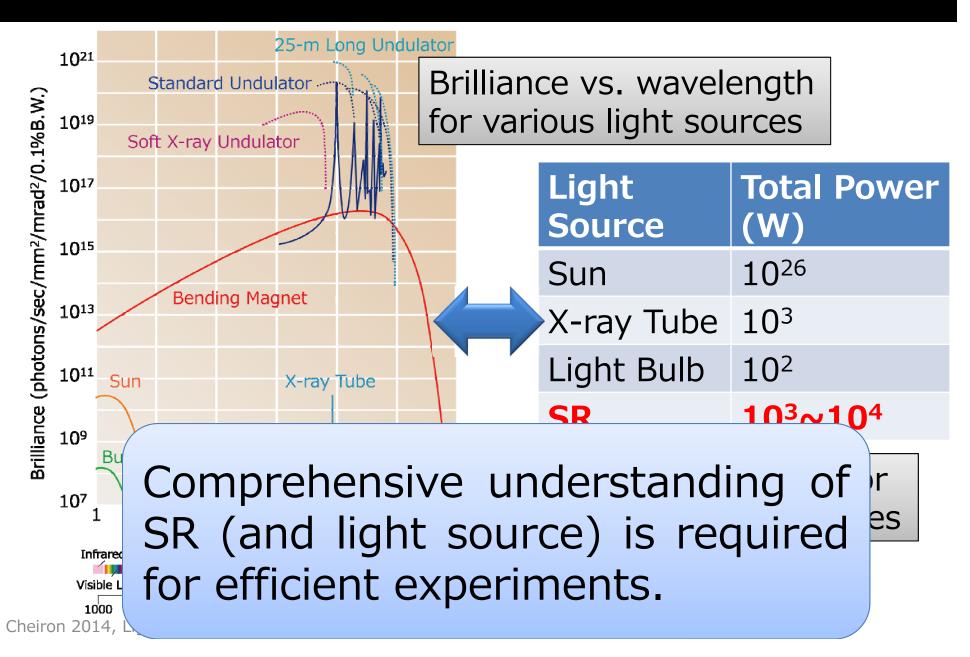
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Overview of SR Facility



What's the Advantage of SR?



Topics in This Lecture (1)

- Fundamentals of Light and SR
 - General description of light
 - Why we need SR?
 - Physical quantity of light
 - Uncertainty of light: Fourier and diffraction limits
 - SR: Light from a moving electron
- Overview of SR Light Source
 - Types of light sources
 - Magnet configuration

Topics in This Lecture (2)

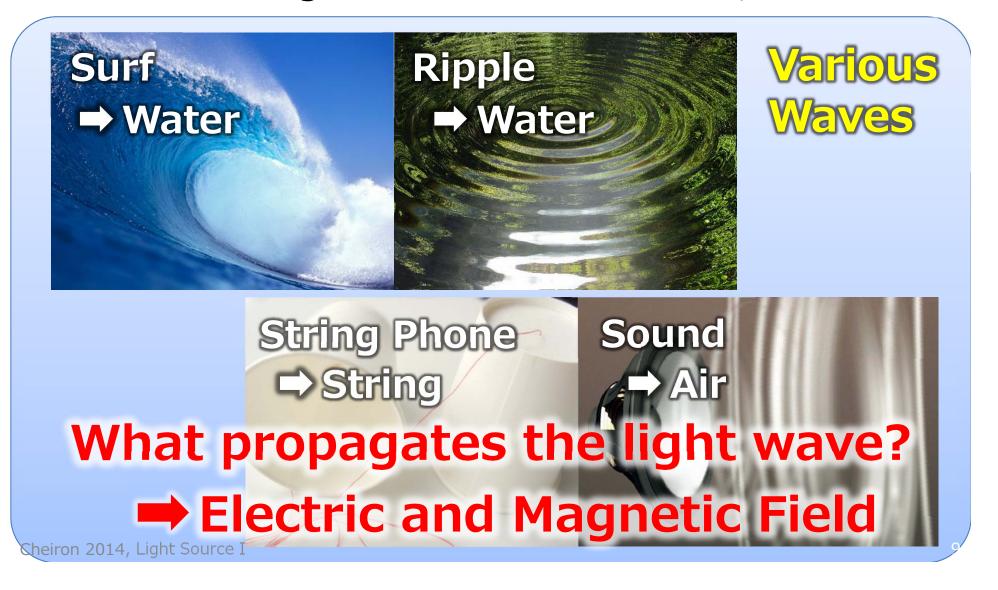
- Characteristics of SR
 - Radiation from bending magnets
 - Electron Trajectory in insertion devices
 - Radiation from insertion devices
- Practical Knowledge on SR
 - Finite emittance and energy spread
 - Heat load and photon flux
 - Evaluation of optical properties of SR
 - Definition of undulators and wigglers
 - Numerical examples

Outline

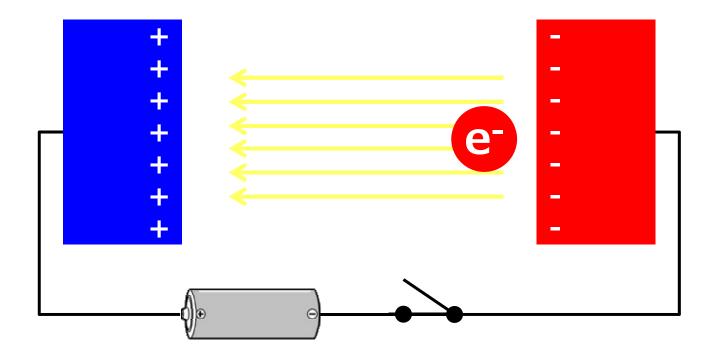
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What is Light?

What is light? It is a kind of wave, but...

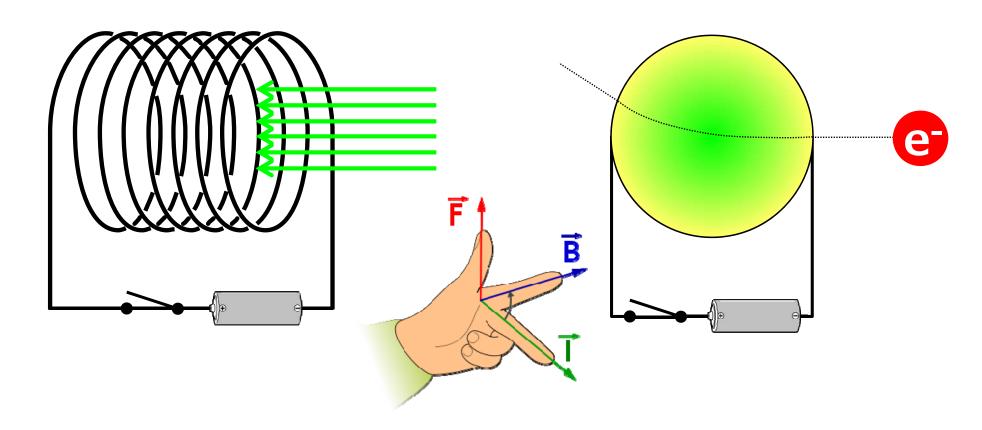


Electric Field



The E-field is generated by electric charges, and gives a force on a charged particle.

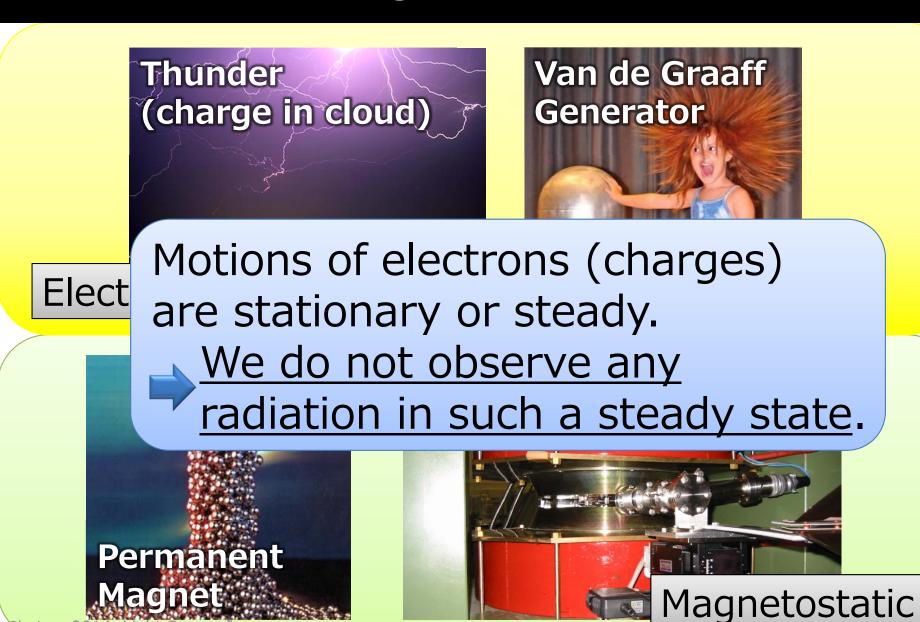
Magnetic Field



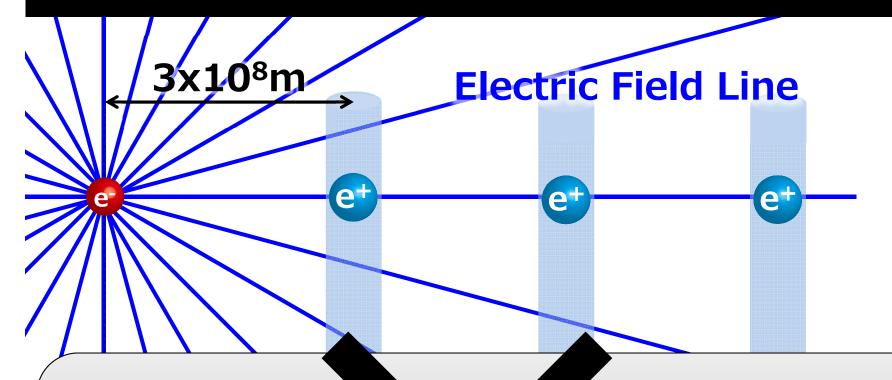
The M-field is generated by moving electric charges, and give a force on a moving charged particle.

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Electro- and Magnetostatic Phenomena



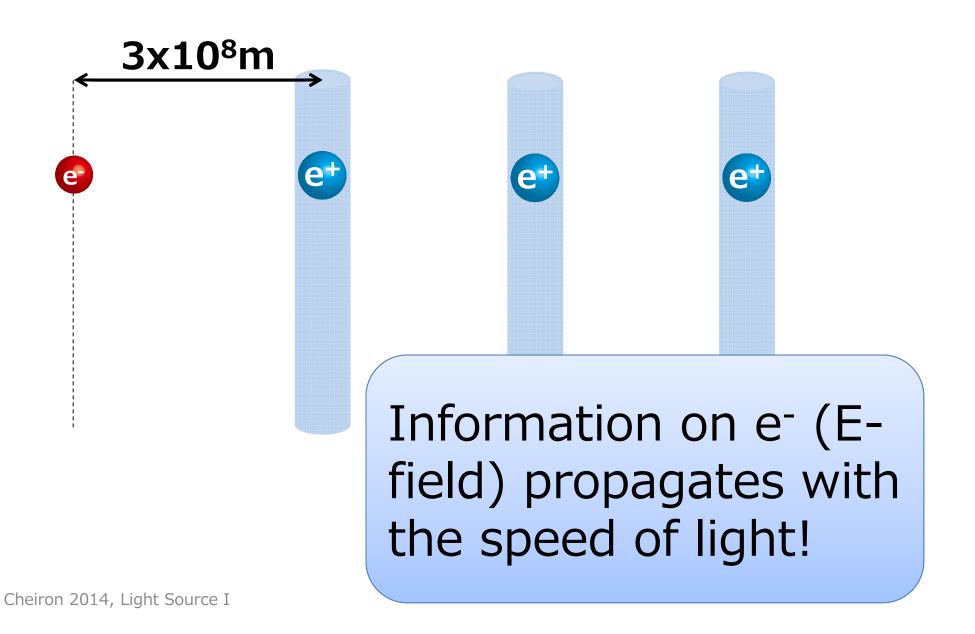
Non-Steady State: Thought Experiment



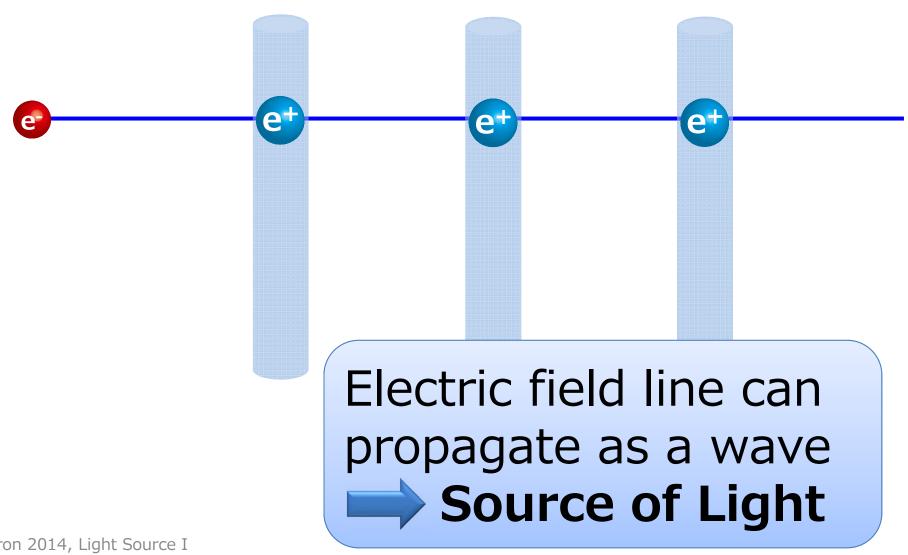
Does e+ moves simulations are propagates

with an infinity specify.

Non-Steady State: Thought Experiment

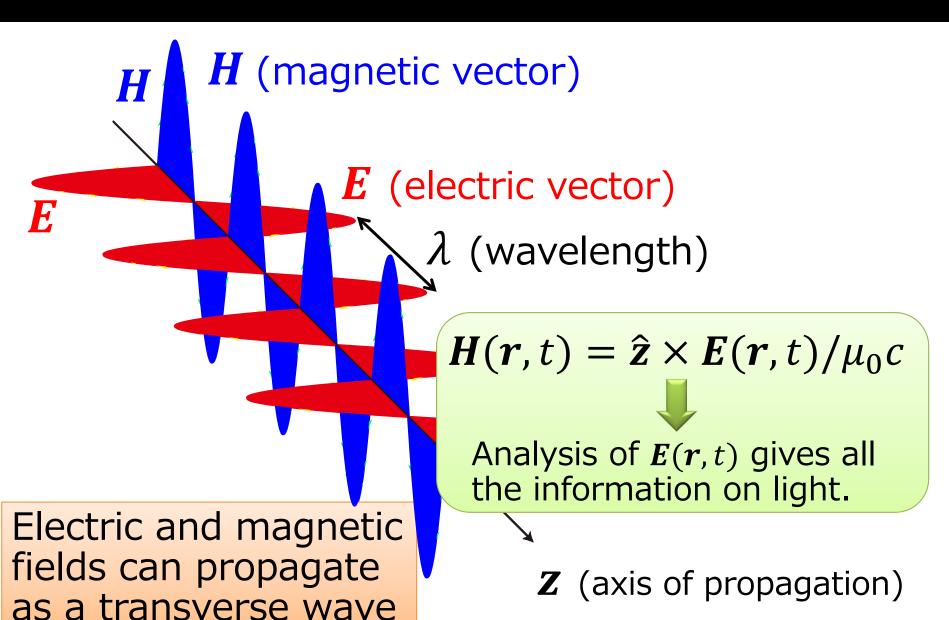


E-Field Line Is Not "Rigid"



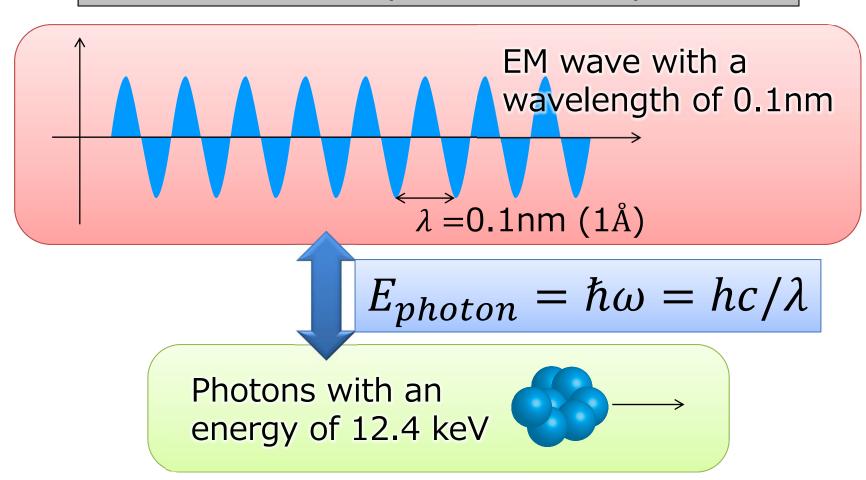
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Light as an Electromagnetic Wave

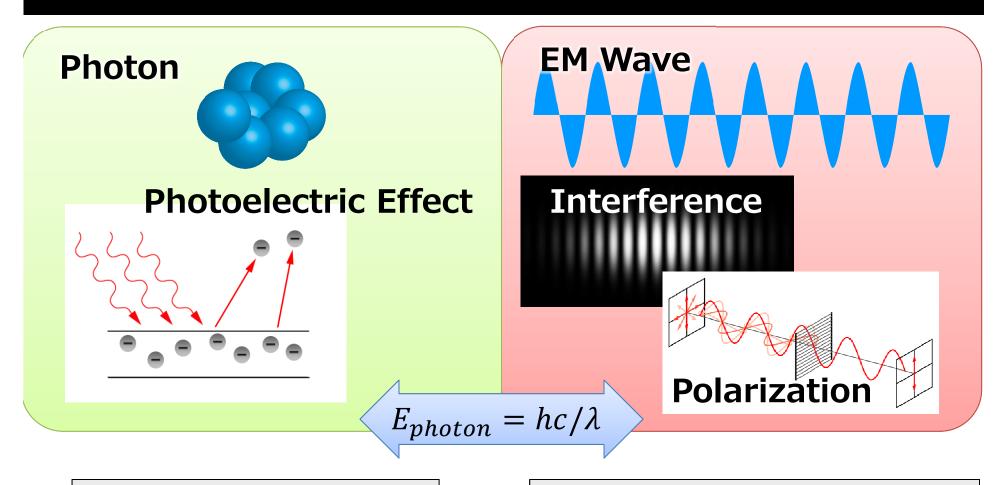


Light as a Photon

Light is not only an electromagnetic wave but also a particle, or a photon.



Wave? Photon?



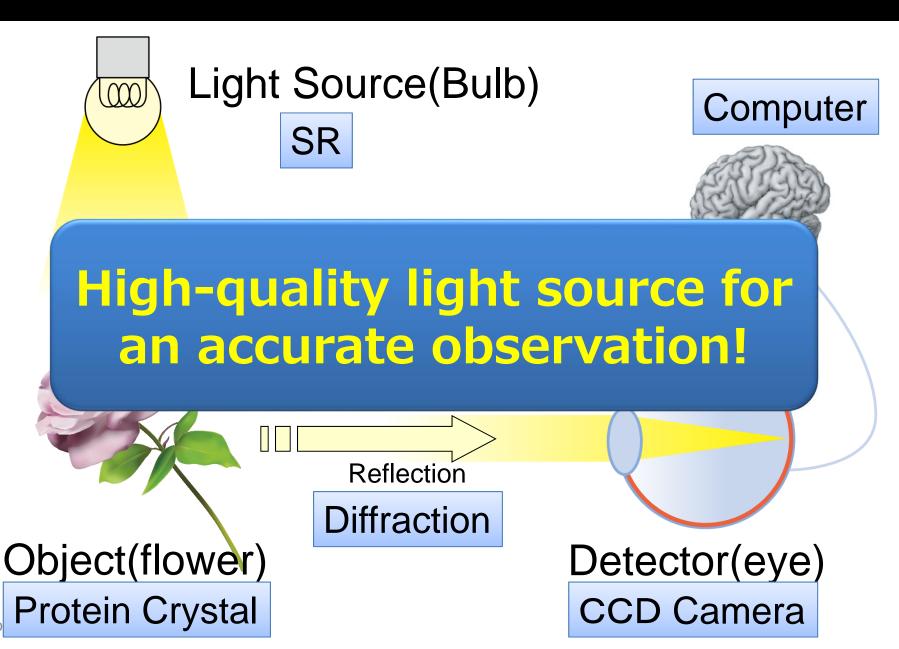
✓ Evaluation of SR characteristics (brilliance, flux, …)

✓ Formulation of SR withI classical electrodynamics (field amplitude)

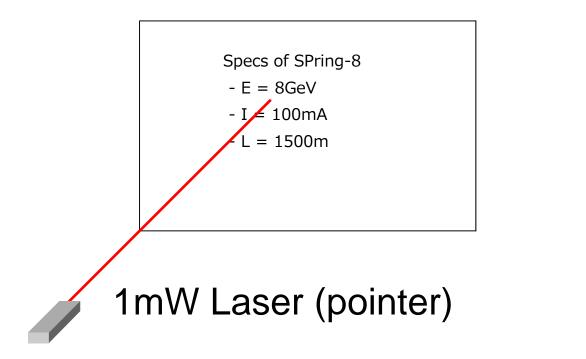
Outline

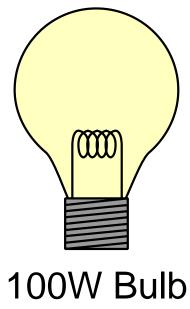
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Observation with Light



Which Quality is Better?





Lighting equipment in a room: **Bulb**Pointer during a presentation: **Laser**



How to Define the Quality of Light?(1)



How to Define the Quality of Light?(2)

Important Features of the Light Source

Item	Object		Why?	
	Flower	Protein		
Radiation Power	0		# Emitted Photons	
Source Size	×		Illuminated Area	
Directivity	\triangle		AlCa	
Monochromaticity		○□	Accuracy of Analysis	
Brilliance				

What is Brilliance?

Brilliance(photons/sec/mm²/mrad²/0.1%B.W.)

Total Power

Source Size x Angular Divergence x Band Width

- Brilliance specifies the quality of light for observation of microscopic objects.
- The brilliance of a light source with a high total power is not necessarily high.

Example of Brilliance Estimation

Item	Bulb	Laser Pointer
Total Power (W)	100	10-3
Angular Div. (mrad²)	$4\pi \times 10^{6}$	1
Source Size: (mm ²)	10 ²	1
Bandwidth: (%)	100	0.01
Brilliance	~108	$\sim 10^{16}$
(photons/sec/)		

Laser is the best light source to observe the microscopic object!

X ray as a Probe

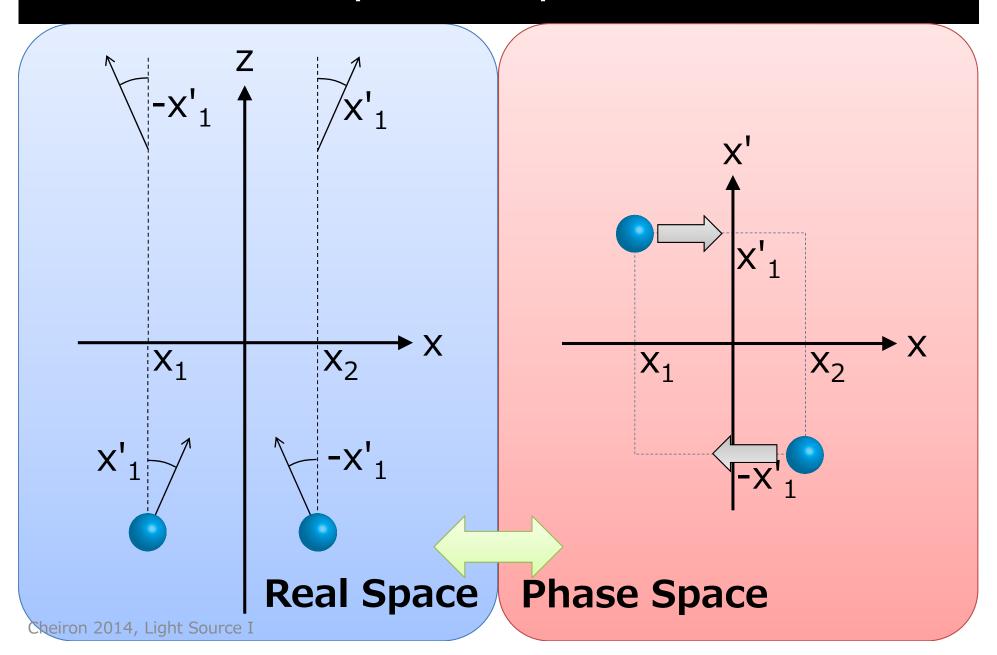
- Definition (not unique)
 - Electromagnetic wave (= light) with I of $10 \text{ nm} (10^{-8} \text{ m}) \sim 0.1 \text{ Å} (10^{-11} \text{ m})$
- Properties
 - High Energy/Photon
 - High Penetration (Roentgen etc..)
- Application to Microscopic Objects
 - X-ray Diffraction
 - Fluorescent X-ray Analysis
- No Practical Lasers!! (until recently)



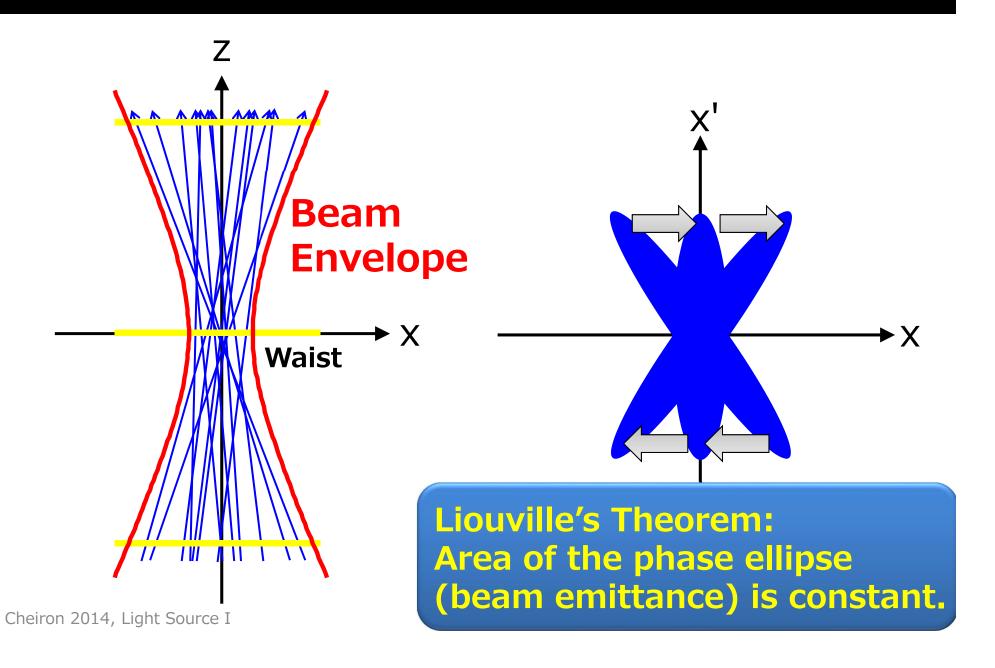
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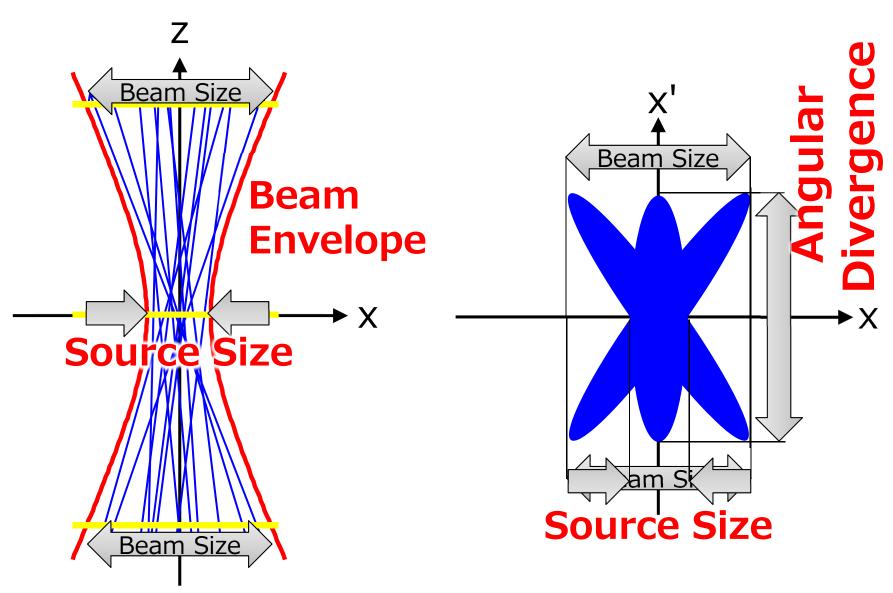
Phase Space Representation



Photon Propagation in Phase Space

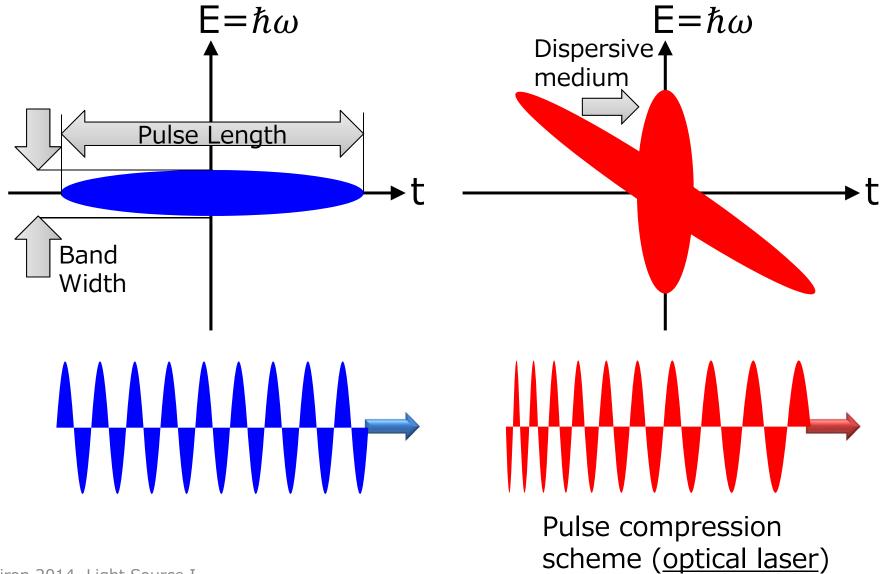


Photon Propagation in Phase Space

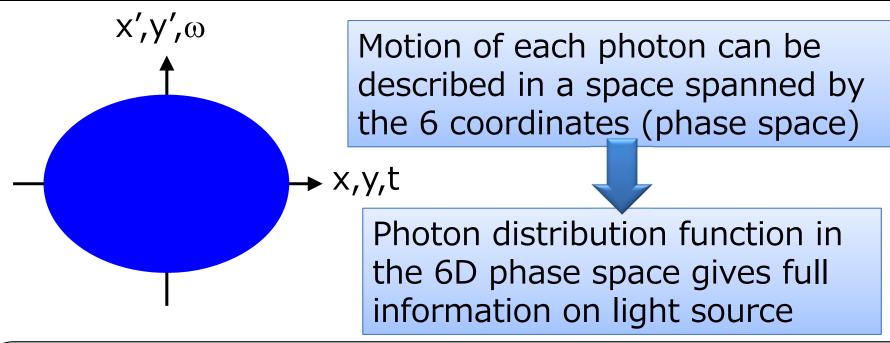


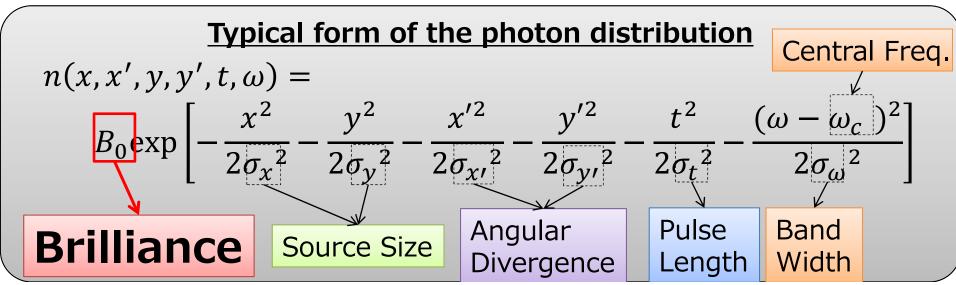
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Energy-Time Phase Space

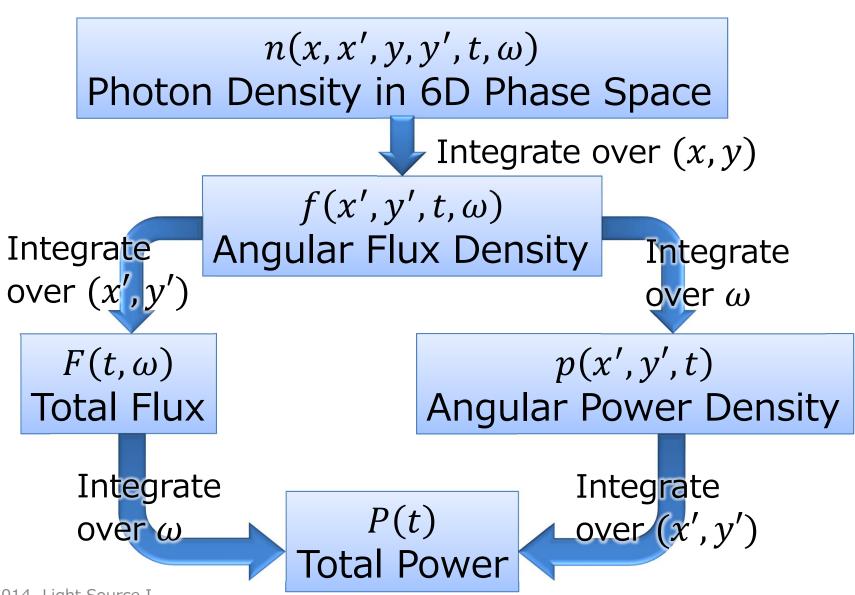


6D Phase Space & Brilliance





Photon Flux & Radiation Power

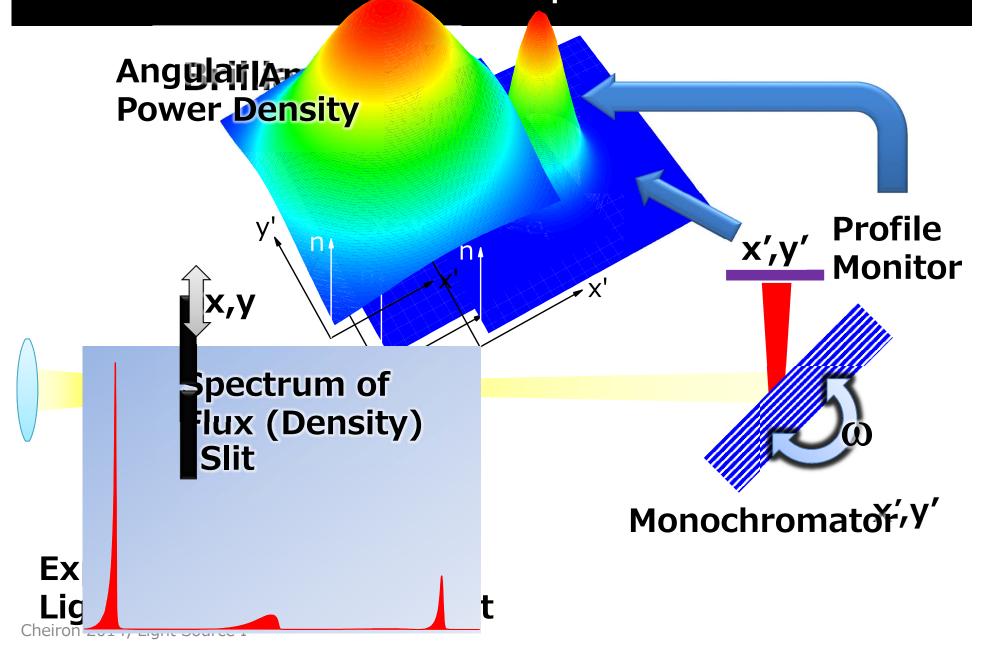


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To Be More Specific...



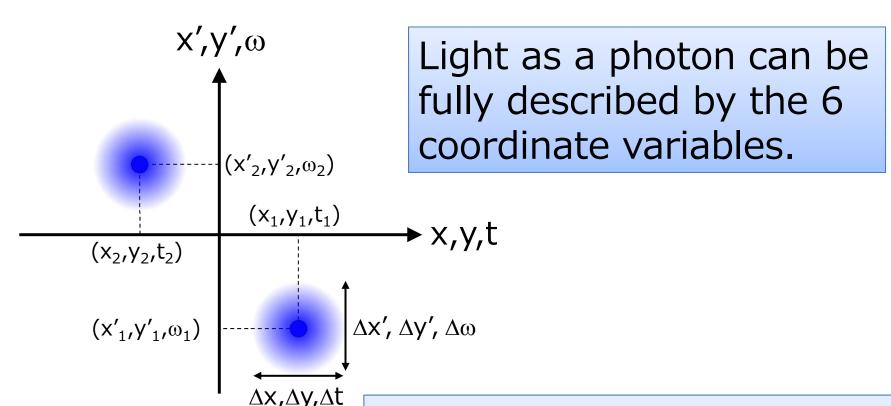
To Be More Specific...



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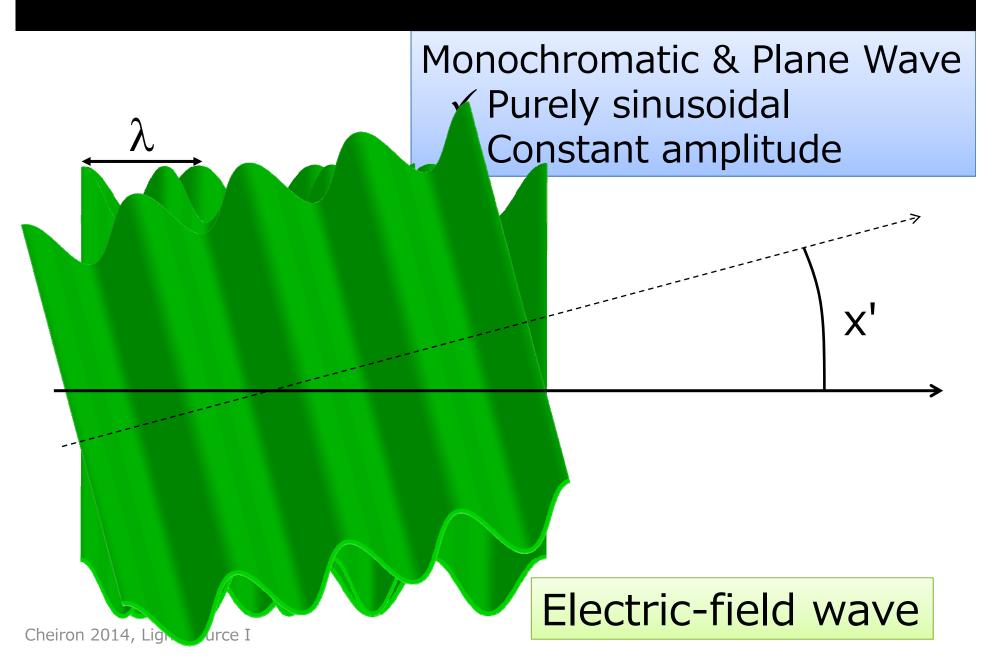
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Uncertainty of Light



Because of the wave nature, they have some uncertainty characterized by the so-called Fourier transform.

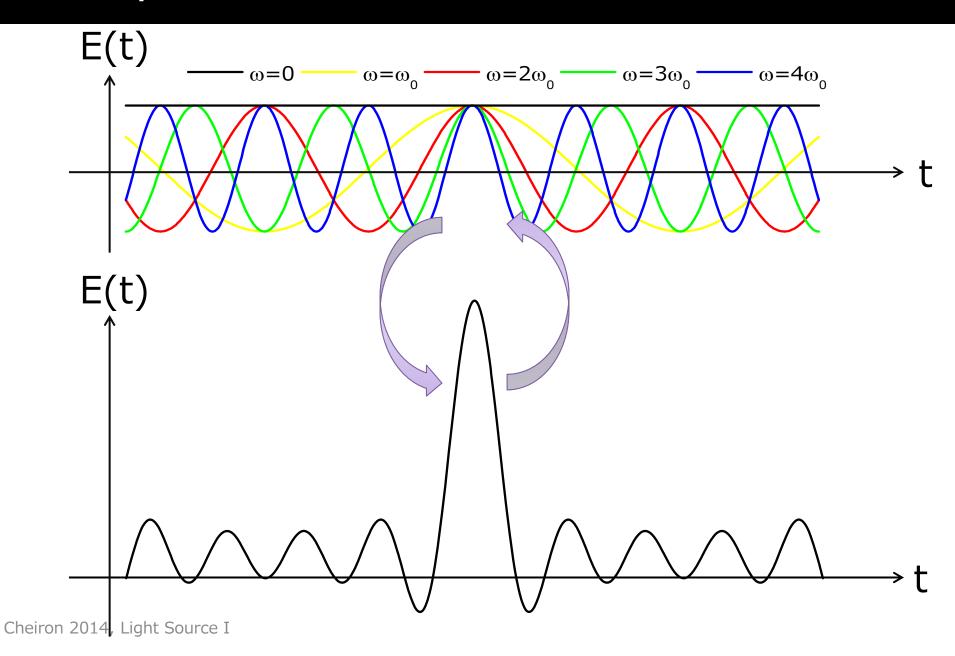
Monochromatic & Plane Wave



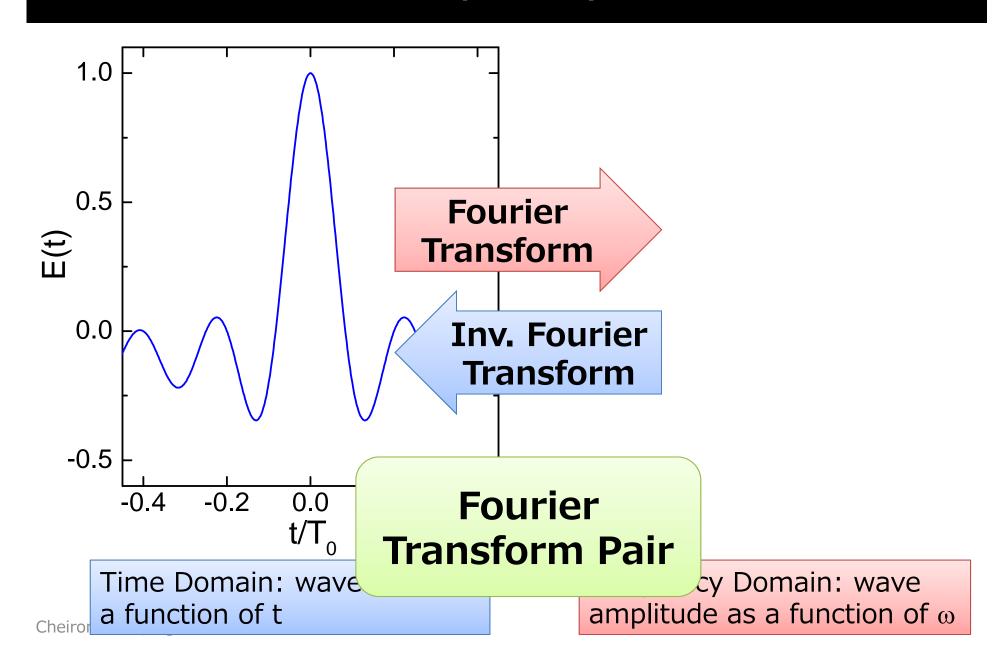
In Reality...

- A monochromatic and plane wave is an (ideal) form of a wave.
- In practice, a wave is composed of many ideal waves having different λ and x'.
- Fourier Transform is a mathematical operation to decompose an arbitrary wave into a number of monochromatic and plane waves.

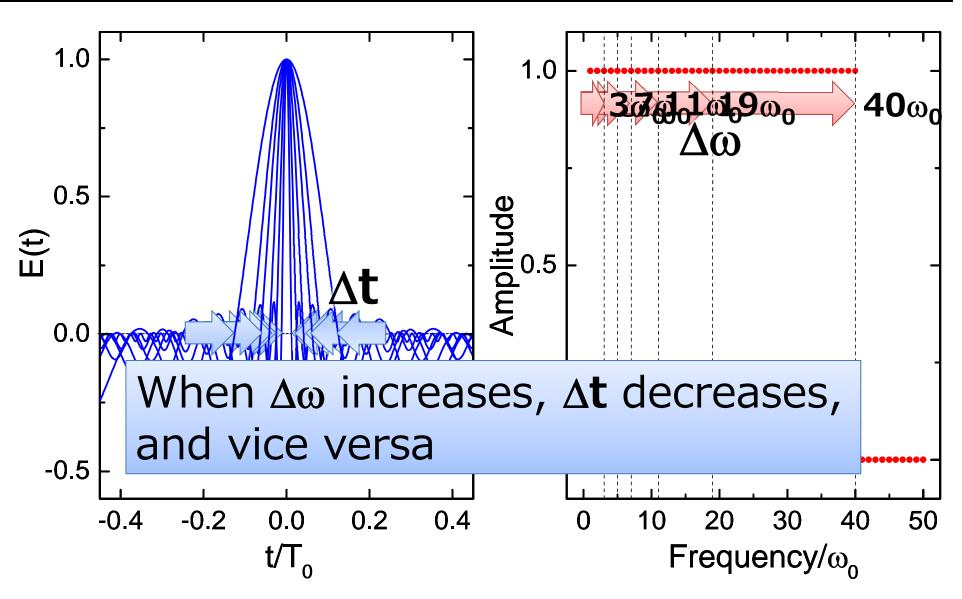
Composition of Monochromatic Waves



Time & Frequency Domains

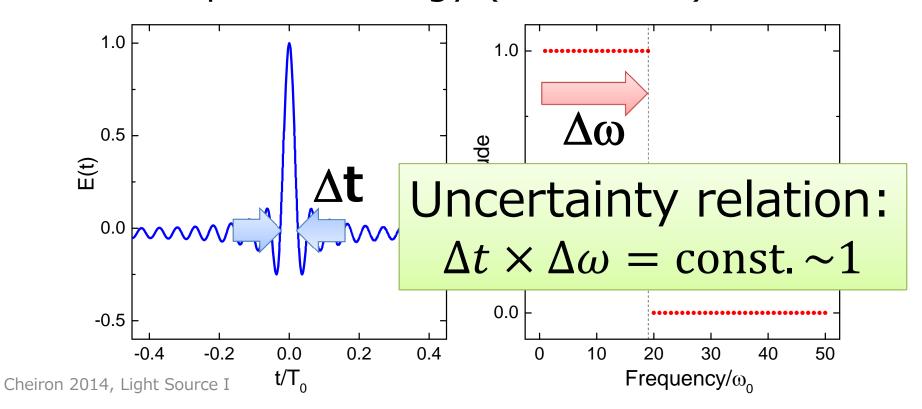


How Does the Waveform Changes?

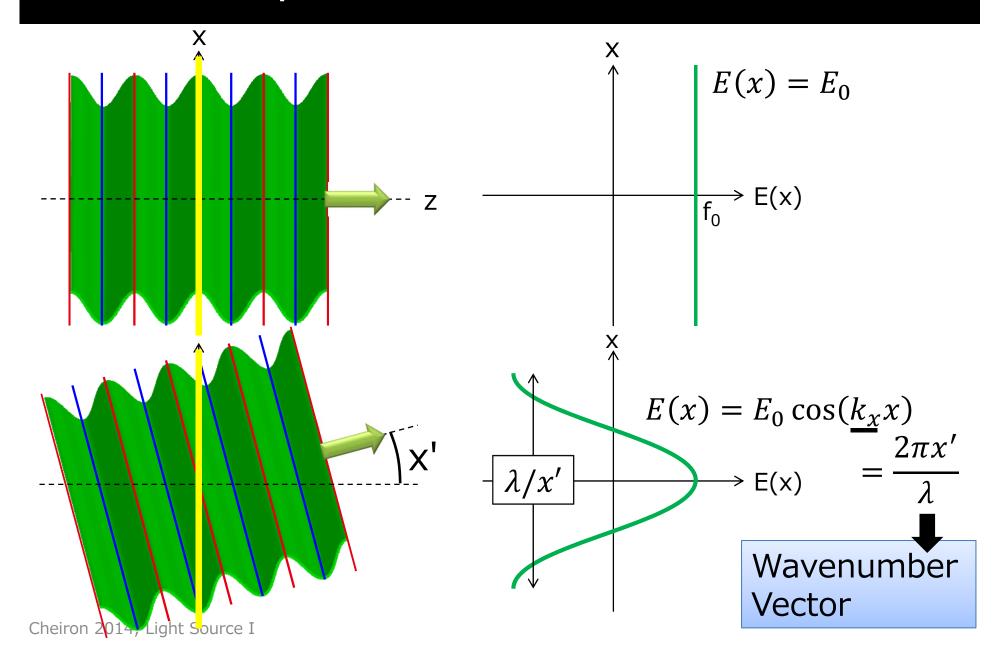


Uncertainty Relation

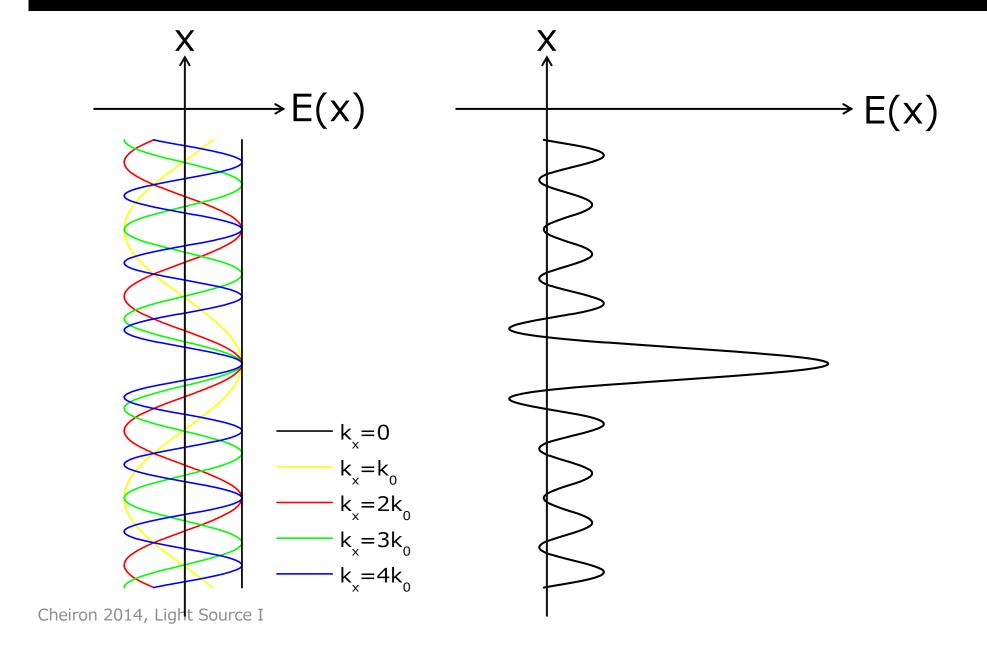
- Δt and $\Delta \omega$ are regarded as uncertainty of a photon
 - $-\Delta t$: longitudinal position (pulse width)
 - $-\Delta\omega$: photon energy (bandwidth)



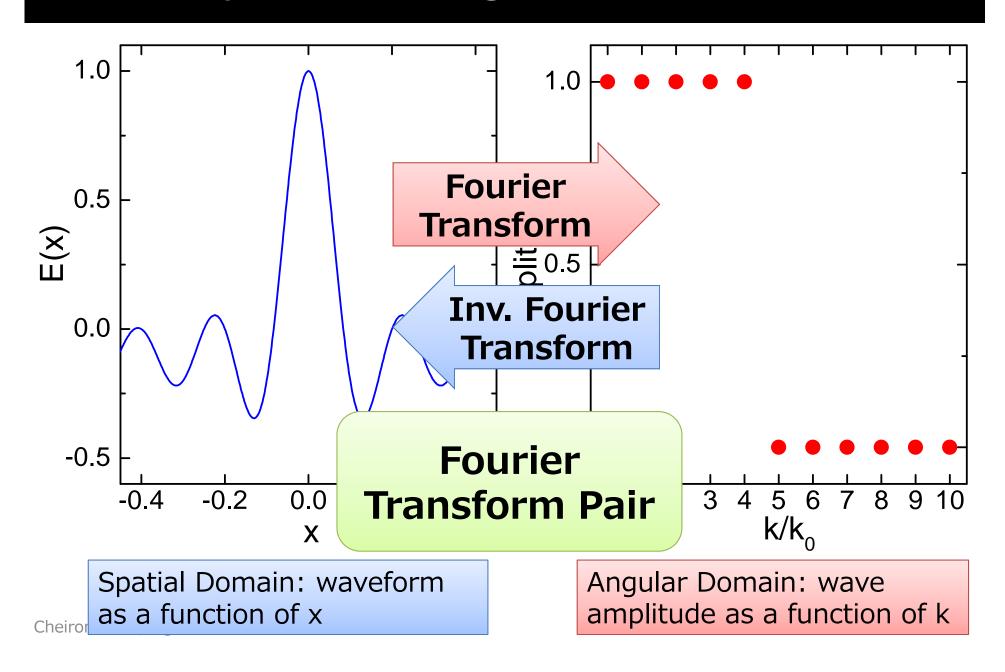
Composition of Plane Waves



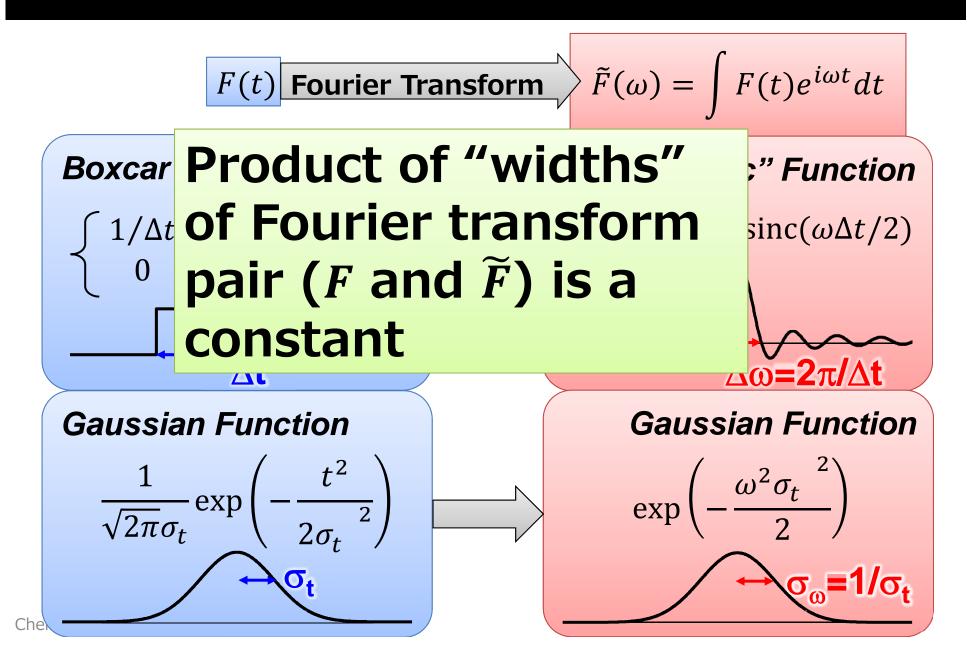
Composition of Plane Waves



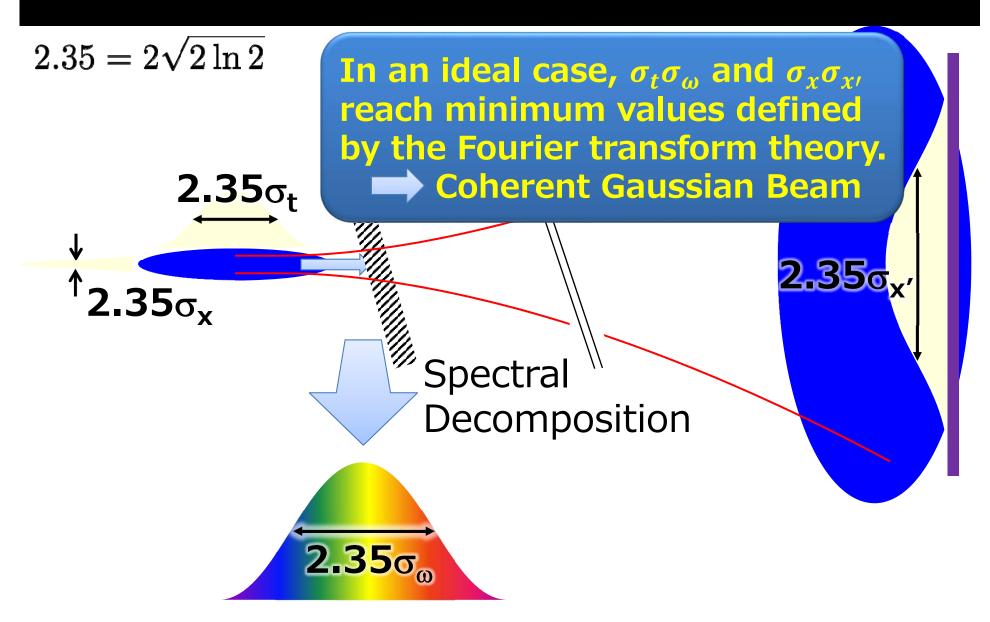
Spatial & Angular Domains



Fourier Transform Examples



Coherent Gaussian Beam



Fourier and Diffraction Limits

	Condition	Extreme Cases	
Fourier Limit	a) temporal $\sigma_t \sigma_\omega \ge \frac{1}{2}$	$\sigma_t = 0$ $\sigma_\omega = \infty$	White (or Pulse) Light
		$\sigma_t = \infty$ $\sigma_\omega = 0$	Monochromatic Light
Diffraction Limit	b) spatial $\sigma_{x}\sigma_{x'} \geq \frac{\lambda}{4\pi}$ $\sigma_{y}\sigma_{y'} \geq \frac{\lambda}{4\pi}$	$\sigma_{\chi} = \infty$ $\sigma_{\chi\prime} = 0$	Parallel Light
		$\sigma_{\chi} \sim \lambda$ $\sigma_{\chi\prime} \sim 1$	Minimum Focal Size

- If equality a) holds, the light is:
 - Temporally Coherent or Fourier Limited
- If equality b) holds, the light is:
 - Spatially Coherent or Diffraction Limited

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SR: Light from a Moving Electron

- Unlike the ordinary light source (sun, light bulb,...), the light emitter of SR (electron) is ultra-relativistic.
- The characteristics of SR is thus quite different because of relativistic effects.
- What we have to take care is:
 - 1. Speed-of-light limit
 - 2. Squeezing of light pulse
 - 3. Conversion of the emission angles

Speed-of-Light Limit

Within the framework of relativity, the velocity of any object never exceeds the speed of light.

$$v/c = \beta = \sqrt{1 - \gamma^{-2}}$$

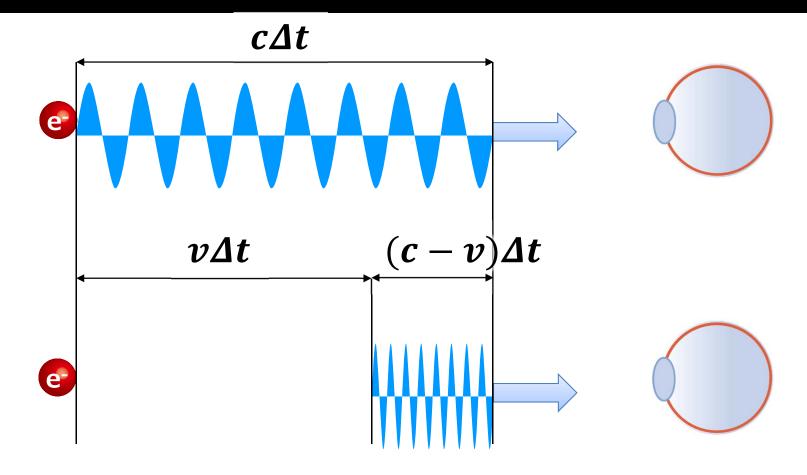
$$\sim 1 - \frac{1}{2\gamma^2}$$

Energy	β
1MeV	0.941
10MeV	0.9988
100MeV	0.999987
8GeV	0.99999998

$$\gamma = rac{E}{mc^2}$$

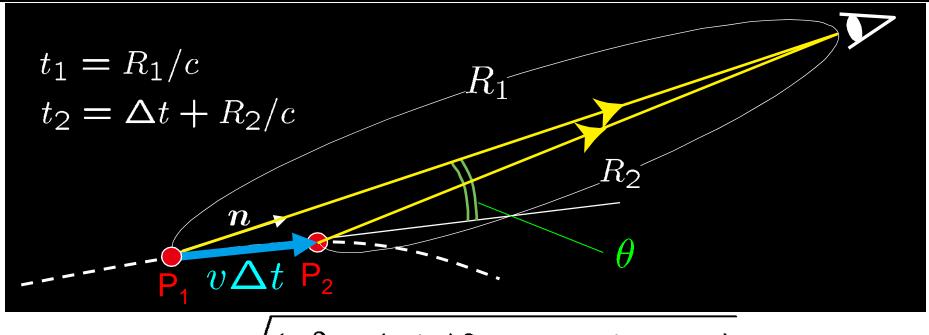
:Lorentz Factor (relative electron energy, mc²=0.511MeV)

Squeezing of Light Pulse Duration



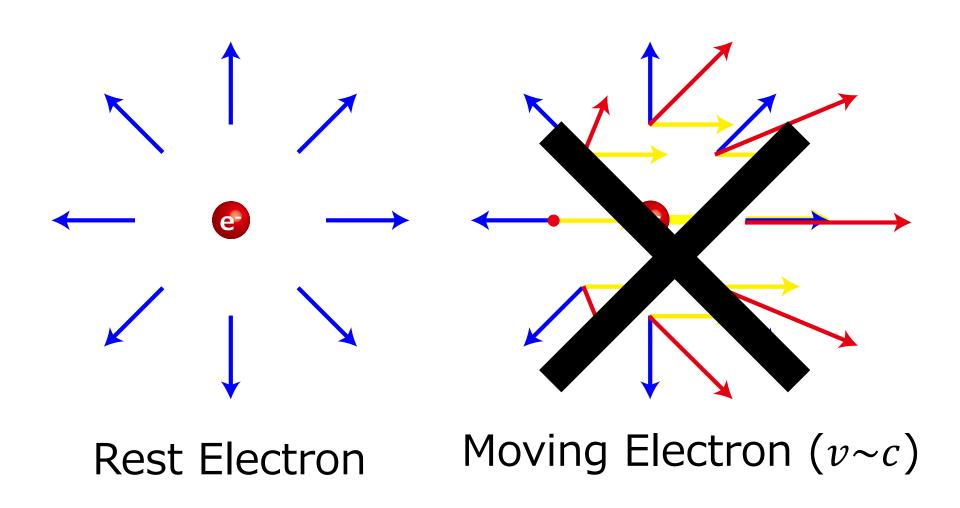
Pulse Duration Ratio =
$$\frac{(c-v)\Delta t}{c\Delta t} = 1 - \beta \sim \frac{1}{2\gamma^2}$$

More Generally...

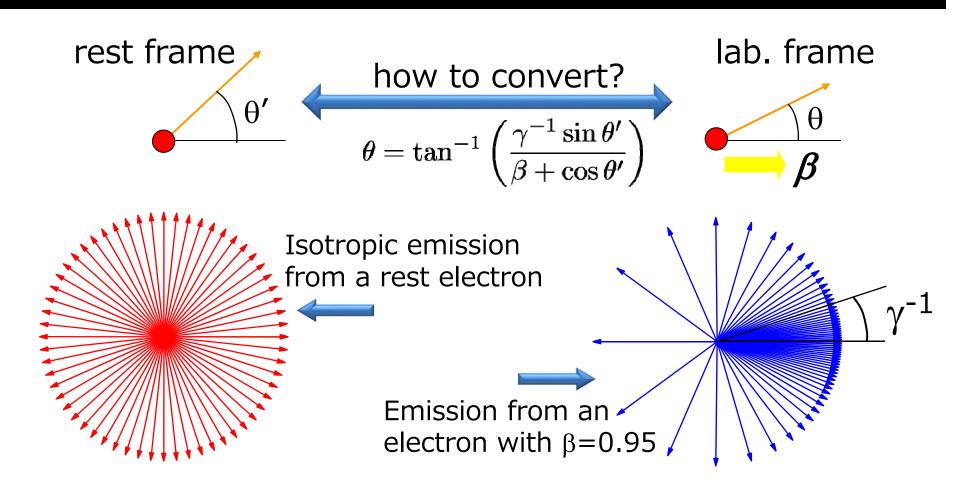


$$R_2 = \sqrt{(R_1^2 + (v\Delta t)^2 - 2R_1v\Delta t\cos\theta)}$$
 $\sim R_1 - (\boldsymbol{v}\cdot\boldsymbol{n})\Delta t$
 $\Delta au = t_2 - t_1 = \Delta t + R_2/c - R_1/c$
 $= \Delta t \frac{(1-oldsymbol{eta}\cdot\boldsymbol{n})}{1-oldsymbol{G}\cdot\boldsymbol{n}} = \Delta t \frac{1}{2\gamma^2} + \theta^2$
 $\gamma > 1, \theta \sim 0$
Time Squeezing

Photons Emitted by a Moving Electron



Conversion of Emission Angles



Light emitted from a moving object $(\beta \sim 1)$ concentrates within γ^{-1}

SR from a High-Energy Electron

