Light Sources II

Takashi TANAKA RIKEN SPring-8 Center

Outline

- Introduction
- Fundamentals of Light and SR
- Overview of SR Light Source
- Characteristics of SR (1)
- Characteristics of SR (2)
- Practical Knowledge on SR

What is SR Light Source?

Magnets to deflect the electron beam and generate SR.



Bending Magnet

- One of the accelerator components in the storage ring.
- Generate **uniform field** to guide the electron beam into a **circular orbit**.
- EMs combined with highly-stable power supplies are adopted in most BMs to satisfy the stringent requirement on field quality and stability.
- Superconducting magnets are used in a few facilities in pursuit of harder x rays.

Insertion Device

- Installed (inserted) into the straight section of the storage ring between two adjacent BMs.
- Generate a periodic magnetic field to let the injected electron beam move along a periodic trajectory.
- Most IDs are composed of PMs, while EMs are used for special use such as helicity switching.
- Two types: wiggler and undulator

Magnetic Circuit of IDs



In each type, a sinusoidal magnetic field is obtained: $B_y(z) \sim B_0(B_r, g/\lambda_u) \sin\left(\frac{2\pi z}{\lambda_u}\right)$

Example of ID Magnets

Halbach-type Magnet Array for SPring-8 Standard Undulators



Example of SR Image

BL41XU@SP-8, first image of SR with a fluorescent screen (<0.1mA)



Comparison of SR Light Sources



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Directionality of BM Radiation



Pulse Structure of BM Radiation



Pulse Structure of BM Radiation



What's the Pulse Duration?



Spectrum of BM Radiation



✓ BM radiation has a white spectrum reaching the frequency of Δω~1/Δτ~γ³c/ρ
 ✓ ω_c = ³/_{2Δτ} = ^{3γ³c}/_{2ρ} ("critical frequency") gives a criterion for BM spectrum.
 ✓ In practical units, ħω_c(keV) = 0.665E² (GeV²)B(T)

Cheiron 2

Example of Spectrum



Angular Profile of BM Radiation



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Coordinate Systems



Field Integrals

$$\frac{d\boldsymbol{P}}{dt} = m\gamma \frac{d\boldsymbol{v}}{dt} = -e\boldsymbol{v} \times \boldsymbol{B}$$

Equation of motion of an electron moving in a magnetic field **B**

$$\left\{egin{aligned} m\gamma\dot{v_x} &= -e(v_yB_z - v_zB_y)\ m\gamma\dot{v_y} &= -e(v_zB_x - v_xB_z)\ u &= u\gamma rac{dv_{x,y}}{v_zdt} = m\gammarac{dv_{x,y}}{dz} = \pm eB_{y,x} \end{aligned}
ight.$$

$$\beta_{x,y} = \pm \frac{e}{\gamma mc} \int^{z} B_{y,x}(z') dz' \equiv \pm \frac{e}{\gamma mc} I_{1y,1x}(z)$$

$$x_{e}, y_{e} = \pm \frac{e}{\gamma mc} \int^{z} dz' \int^{z'} B_{y,x}(z'') dz'' \equiv \pm \frac{e}{\gamma mc} I_{2y,2x}(z)$$

$$I_{1,} I_{2}: 1 \text{st and 2nd field integrals of the ID}$$

Trajectory in an Ideal ID



Effects due to the ID Magnetic Field

transverse
$$\beta_x(z) = \frac{K}{\gamma} \cos\left(\frac{2\pi z}{\lambda_u}\right)$$

longitudinal $\beta_z = \sqrt{\beta^2 - \beta_x^2}$
velocity
 $= 1 - \frac{1}{2\gamma^2} - \frac{K^2}{4\gamma^2} - \frac{K^2}{4\gamma^2} \cos\left(\frac{4\pi z}{\lambda_u}\right)$
Original value
Average Value $\overline{\beta_z}$
ID field induces:
 \checkmark transverse (x) oscillation
 \checkmark longitudinal (z) oscillation
 \checkmark effective deceleration ($\Delta\beta_z = K^2/4\gamma^2$)

General Form of Time Squeezing

$$\begin{aligned} \frac{d\tau}{dt} &= 1 - \boldsymbol{\beta} \cdot \boldsymbol{n} \\ & \boldsymbol{\beta}_z &= \sqrt{\beta^2 - \beta_x^2 - \beta_y^2} \\ & \boldsymbol{\beta}_z &= \sqrt{\beta^2 - \beta_x^2 - \beta_y^2} \\ & \boldsymbol{\gamma}_z &\sim 1 - (\gamma^{-2} + \beta_x^2 + \beta_y^2)/2 \\ & \boldsymbol{n}_z &\sim 1 - (\theta_x^2 + \theta_y^2)/2 \end{aligned}$$
$$= \frac{1}{2\gamma^2} + (\theta_x - \beta_x)^2 + (\theta_y - \beta_y)^2 \end{aligned}$$

Time squeezing takes place most significantly when the electron is moving in the direction of observation ($\beta = \theta$).

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Wiggler Radiation

- Wiggler radiation (WR) is regarded as incoherent sum of SR emitted at each position of wiggler.
 - Summation as photons in the framework of geometrical optics.



Photon Distribution in Phase Space



Beam Waist Position

- Larger *N* results in larger area of photon distribution in the phase space, i.e., larger emittance.
- B does not linearly depend on N

Comparison with BM Radiation



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Fundamental Wavelength of UR



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UR with Infinite Periods

• If the undulator length is infinite, the pulse duration is infinitely long, and thus the radiation is completely monochromatic with line spectrum.

$$f(\theta,\omega) = \delta(\omega - \omega_1) = \delta\left(\omega - \frac{4\pi c \gamma^2 / \lambda_u}{1 + K^2 / 2 + \gamma^2 \theta^2}\right)$$

• In practice, the undulator length is finite, so the line spectrum is broadened.



Effects due to Finite Periods



Brief Note on UR Formulae

- In the previous derivations of UR spectral function, no knowledge on electrodynamics is required.
- In practice, *E*₀ is a complicated function of θ and K, and needs to be calculated by Fourier transforming the electric field derived from the Lienard-Wiecherd potential.
- However, the simple derivation gives us a clear understanding on UR properties.

Energy Spectrum of UR



Angular Profile of UR



Angular Divergence of UR



Source Size of UR



Longer device results in smaller angular divergence & larger source size, but the emittance does not change.

Higher Harmonics

Photons with at $n\omega_1$ are observed as well as at ω_1 , where *n* is an integer.















Mechanisms of Higher Harmonics



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Effective Properties of SR

- Properties of SR emitted from an e⁻ beam are different from those from a single e⁻.
- They are referred to as "effective" properties of SR, as opposed to "natural" properties.



Example in SPring-8: E-t Phase Space



Example in SPring-8: (x,y) Space



Example in SPring-8: (x',y') Space



Convolution Between e- and Photon



Spectral Profile (UR)



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Angular & Spatial Profile (UR)



Heat Load on Optical Elements

- SR is usually processed by several optical elements before irradiation to the sample, such as the focusing mirror, monochromator.
- These elements can be easily damaged by the heat load of SR.
- In the case of UR, the heat load can be reduced by taking advantage of the difference in the angular profile of the photon flux and radiation power.

Spatial Profile of Power and Flux (UR)



The power profile is much broader than the flux. Extraction of SR with an appropriate slit is thus effective.

What's the Optimum Aperture Size?



Wiggler? Undulator? (1)

- Wigglers are identical to undulator from the point of view of magnetic circuit.
- It is generally said that the K value distinguishes between the two, however, this is not exactly correct.
- What we should take care is the photon energy region of interest.

Wiggler? Undulator? (2)



Undulator Radiation Gallery

- For quantitative evaluation of SR, a computer code "SPECTRA" is available.
- SPECTRA also offers a function to "visualize" the computation results for further understanding of SR.
 - brilliance curve & spectrum
 - on- and off-peak angular profiles of flux
 - on- and off-axis spectra
 - effects of opening the slit aperture
 - undulator-to-wiggler transition

Brilliance Curve & Spectrum

Spectrum –, Peak Brilliance 1st – 3rd – 5th –



Opening the Slit Aperture



Cheiron 201



Cheiron 20

Flux Angular Profile

On-Axis Spectrum

Angular Profile (Finite Emittance) (Zero Emittance)

Angular Profile



Undulator-to-Wiggler Transition



Other Important Topics

- Quantitative descriptions of SR
- Light sources for CPR & helicity switching
 - helical undulator & elliptic wiggler
 - chicanes & choppers, kicker magnets
- Effects on the electron beam
 - natural focusing
 - beam-axis fluctuation due to COD variation
- R&Ds toward shorter magnetic period
 - superconducting undulators
 - cryogenic permanent magnet undulators
- Coherent SR for intense THz light
- Undulators for SASE-based X-ray FEL

Announcement

- Those who are going to join the lecture on "SPECTRA" scheduled on Monday evening are recommended to bring your own PC.
- If you do not have any PC, please consult the office.
- Before joining the lecture, download the software from the URL below and finish installation.

http://radiant.harima.riken.go.jp/spectra

Angular Divergence & Source Size

