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# Inelastic X-Ray Scattering

**Selected Slides Only**

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## Scope & Outline

Huge & Complex Topic - Appropriate for a semester, not an hour...

**Main Goal:**  
Introduce Capabilities & Put them in Context  
What properties can be measured?  
Why consider these techniques?

**Outline:**  
Introduction  
Instrumentation  
Non-Resonant  
Resonant  
Others (time permitting)

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## Some References

Shulke, W. (2007), *Electron Dynamics by Inelastic X-Ray Scattering*.  
New York: Oxford University Press.  
**& References therein (RIXS, X-Ray Raman, NRIXS...)**

Squires, G. L. (1978). *Introduction to the Theory of Thermal Neutron Scattering*.  
New York: Dover Publications, Inc.

van Hove, L. (1954). *Phys. Rev.* **95**, 249-262.

Born, M. & Huang, K. (1954). *Dynamical Theory of Crystal Lattices*.  
Oxford: Clarendon press.

Bruesch, P. (1982). *Phonons: Theory and Experiments*, Springer-Verlag.

Cooper, M.J. (1985). *Compton Scattering Rep. Prog. Phys.* **48** 415-481

Ament, L.J., et al, (2011). *RIXS, Rev. Mod. Phys.* **83** 705-767

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## Scientific Information

(from IXS)

**Atomic Dynamics <-> Motions of atoms in a solid (phonons) or liquid.**  
Phase transitions, thermal properties, fundamental science (Atomic binding)  
Electron-phonon coupling, Magneto-elastic coupling  
Superconductors, Ferroelectrics, multiferroics, etc

**Electronic Dynamics <-> Motions/transitions of electrons**  
Chemical Bonding (Valence, etc)  
Electronic Energy Levels (atomic/molecular)  
Delocalized Electronic Excitations  
Generalized Dielectric Response  
Fermi-Surface Topology  
Magnetic structure  
Complex Materials

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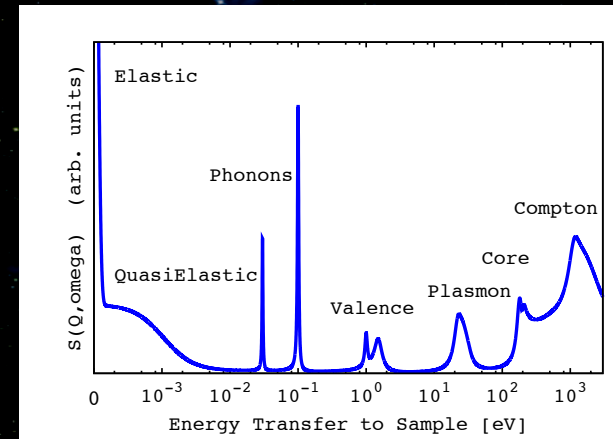
# Table Of IXS Techniques/Applications

Technique	Comment	Energy Scale	Information
X-Ray Raman	(E)XAFS in Special Cases	$E_{in} \sim 10$ keV $\Delta E \sim 100-1000$ eV	Edge Structure, Bonding
Compton	Oldest Note: Resolution Limited	$E_{in} \sim 150$ keV $\Delta E \sim$ keV	Electron Momentum Density Fermi Surface Shape
Magnetic Compton	Weak But Possible	$E_{in} \sim 150$ keV $\Delta E \sim$ keV	Density of Unpaired Spins
RIXS Resonant IXS	High Rate Somewhat Complicated	$E_{in} \sim 4-15$ keV $\Delta E \sim 1-50$ eV	Electronic Structure
SIXS Soft (Resonant) IXS	Exploding, Huge Instruments Surface Sensitivity	$0.1-1.5$ keV $\Delta E \sim 0.05-5$ eV	Electronic & Magnetic Structure
NRIXS Non-Resonant IXS	Low Rate Simpler	$E_{in} \sim 10$ keV $\Delta E \sim <1-50$ eV	Electronic Structure
IXS High-Resolution IXS	Large Instrument	$E_{in} \sim 16-26$ keV $\Delta E \sim 1-100$ meV	Phonon Dispersion
NIS Nuclear IXS	Atom Specific Via Mossbauer Nuclei	$E_{in} \sim 14-25$ keV $\Delta E \sim 1-100$ meV	Element Specific Phonon Density of States (DOS)

Note:  $\Delta E$  = Typical Energy Transfer (Not Resolution)  
Note also: Limit to FAST dynamics ( $\sim 10$  ps or faster)

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# Excitation Energy Scales

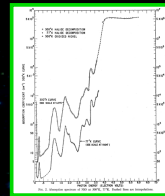


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# Spectroscopy Absorption vs. Scattering

Absorption Spectroscopy  
Optical, IR, NMR  
Raman

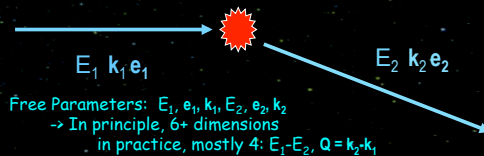
Measure absorption as you scan the incident energy  
When energy hits a resonance, or exceeds a gap, or... get a change



Optical Spect. NiO  
Newman, PR 1959

Free Parameters:  $E_1, e_1, k_1$   
→ In principle, 3+ dimensions  
but in practice mostly 1 ( $E_1$ )

Scattering Spectroscopy  
IXS, INS

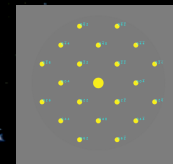


Scattering is more complex, but gives more information.  
Energy scales PLUS spatial structure on scale of probe wavelength

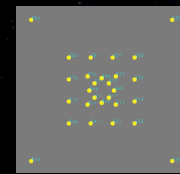
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# Where We Are Measuring Between the Bragg Peaks...

Conventional Diffraction  
Linear Scale

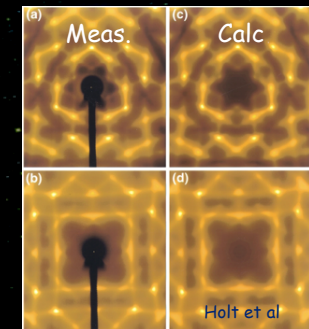


Precession Photo



Laue Photo  
Bragg peaks

On Log Scale



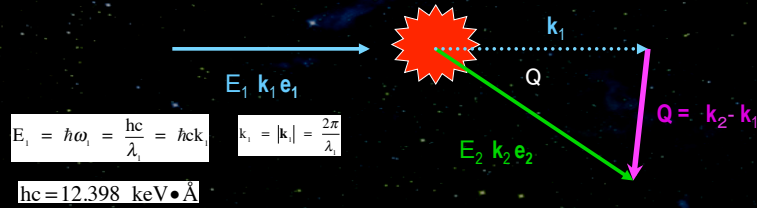
Holt et al

For IXS we are usually measuring between the Bragg peaks where the intensity is weaker.  
A strong signal is down by  $10^7$ , weak by  $10^{11}$

Why...?

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## X-Ray Scattering Diagram



Two Main Quantities:

Energy Transfer

$$E \text{ or } \Delta E = E_1 - E_2 \equiv \hbar\omega$$

Note: For Resonant Scattering  
 $E_1$  and  $E_2$  and Poln.  
Are also important

Momentum Transfer

$$\mathbf{Q} \equiv \mathbf{k}_2 - \mathbf{k}_1$$

$$Q \equiv |\mathbf{Q}| \approx \frac{4\pi}{\lambda_1} \sin\left(\frac{\theta}{2}\right)$$

Periodicity  $d = \frac{2\pi}{|\mathbf{Q}|}$

## Resonant vs Non-Resonant

**Resonant:**  
RIXS  
SIXS

Tune near an atomic transition energy  
ie: K, L or M Edge of an atom

Generally High Rate  
Complex interpretation  
Energy fixed by resonance  $\rightarrow$  poorer resolution

**Non-Resonant:**  
IXS  
NRXS

Far from any atomic transition.  
Small cross-section  
Interpretation directly in terms of electron density  
Choose energy to match optics  $\rightarrow$  good Resolution

Different Experimental Setups  $\rightarrow$  Modern Specialization

Nuclear Resonant & Compton Scattering  $\rightarrow$  Different

## Dynamic Structure Factor

It is convenient, especially for non-resonant scattering, to separate the properties of the material and the properties of the interaction of the photon with the material (electron).

$$I_{\text{scattered}}(\mathbf{Q}, \omega) \propto \frac{d^2\sigma}{d\Omega d\omega} = r_e^2 \left( \mathbf{e}_2^* \cdot \mathbf{e}_1 \right)^2 \frac{k_2}{k_1} S(\mathbf{Q}, \omega)$$

$$\sigma_{\text{Thomson}} = r_e^2 \left( \mathbf{e}_2^* \cdot \mathbf{e}_1 \right)^2$$

Thomson Scattering  
Cross Section  
"A Scale Factor"

$$S(\mathbf{Q}, \omega)$$

Dynamic Structure Factor  
"The Science"

## Different Views of $S(\mathbf{Q}, \omega)$

$$S(\mathbf{Q}, \omega) = \sum_{\lambda, \lambda'} p_{\lambda} \left\langle \lambda' \left| \sum_{\text{electrons } j} e^{i\mathbf{Q} \cdot \mathbf{r}_j} \right| \lambda \right\rangle \delta(E_{\lambda'} - E_{\lambda} - \hbar\omega)$$

Transition between states

$$= \frac{1}{2\pi\hbar} \int dt \int d^3r \int d^3r' e^{-i\mathbf{Q} \cdot \mathbf{r}} \left\langle \rho(\mathbf{r}', t=0) \rho^*(\mathbf{r} + \mathbf{r}', t) \right\rangle \rightarrow N \sum_{\mathbf{q}} \sum_{\text{Modes}} \left| \sum_{\text{Atoms } d} \frac{f_d(\mathbf{Q})}{\sqrt{2M_d}} e^{-i\mathbf{W}_d(\mathbf{Q})} \mathbf{Q} \cdot \mathbf{e}_{\mathbf{q}ld} e^{i\mathbf{Q} \cdot \mathbf{r}_d} \right|^2 \delta(\mathbf{Q} - \mathbf{q}) F_{\mathbf{q}}(\omega)$$

Fluctuations in electron density

$$= \frac{1}{\pi} \frac{1}{1 - e^{-\hbar\omega/k_B T}} \text{Im} \{ -\chi(\mathbf{Q}, \omega) \} = \frac{1}{\pi} \frac{1}{1 - e^{-\hbar\omega/k_B T}} \frac{1}{V(\mathbf{Q})} \text{Im} \{ -\epsilon^{-1}(\mathbf{Q}, \omega) \}$$

Generalized Response  
(e.g. Dielectric functions)

See Squires, Lovesy, Shulke, Sinha (JPCM 13 (2001) 7511)

## Why is it Better to Measure in Momentum/Energy Space?

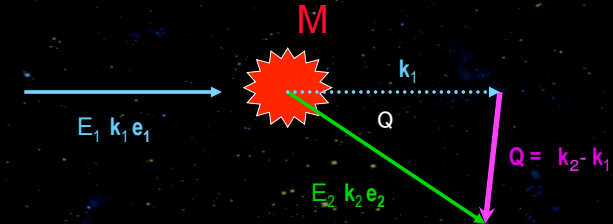
For diffraction (and diffractive/coherent imaging), one goes to great lengths to convert from momentum space to real space.  
If possible, a direct real-space measurement is preferred.

So why

$$S(\mathbf{Q}, \omega)$$

## Kinematics

Conservation of Energy



Kinetic Energy Given to Sample:

$$E_{\text{recoil}} = \frac{p^2}{2M} = \frac{\hbar^2 \mathbf{Q}^2}{2M}$$

Take:  $M=57 \text{ amu}$ ,  $Q/c = 7 \text{ \AA}^{-1} \rightarrow E_r = 2.3 \text{ meV}$

f-sum rule:

$$\frac{\int d\omega \hbar \omega S(\mathbf{Q}, \omega)}{\int d\omega S(\mathbf{Q}, \omega)} = \frac{\hbar^2 \mathbf{Q}^2}{2M}$$

Compton Form:  $\lambda_2 - \lambda_1 = \frac{h}{Mc} (1 - \cos \Theta)$

$$\lambda_c = \frac{h}{m_e c} = 0.0243 \text{ \AA}$$

## The IXS Spectrometer

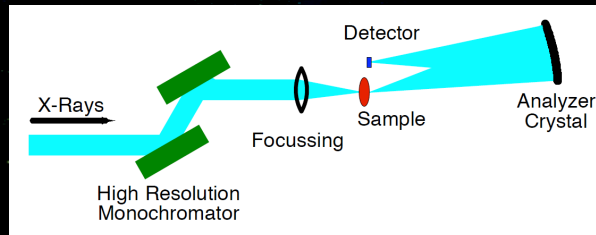
### An Optics Problem

#### Main Components

**Monochromator:**  
Modestly Difficult  
Accepts  $15 \times 40 \text{ } \mu\text{rad}^2$

**Sample Stages**  
Straightforward  
Only Need Space

**Analyzer:**  
Large Solid Angle  
Difficult



The Goal: Put it all together and  
Keep Good Resolution, Not Lose Flux

Note: small bandwidth means starting flux reduced by 2 to 3 orders of magnitude...

## Basic Optical Concept

(Hard x-rays)

Bragg's Law :  $\lambda = 2d \sin(\Theta_B) \Rightarrow \Delta\theta = \tan(\Theta_B) \frac{\Delta E}{E}$

Working closer to  $\Theta_B \sim 90 \text{ deg}$ , maximizes the angular acceptance for a given energy resolution...

Better energy resolution  
→ Closer to 90 degrees  
→ Large Spectrometer

$$\frac{\Delta E}{E} \sim \frac{1}{N_{\text{planes}}}$$

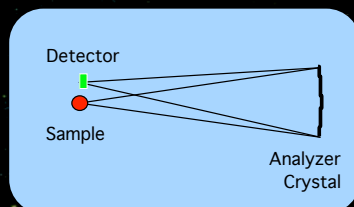


## High Resolution Analyzer Crystals

The more difficult optic...

### Require:

- Correct Shape (Spherically Curved,  $R=9.8$  m)
- Not Strained ( $\Delta E/E \sim \text{few } 10^{-8} > \Delta d/d < \text{few } 10^{-8}$ )



Method: Bond many small crystallites to a curved substrate.

1. Cut

2. Etch

3. Bond to Substrate

4. Remove Back



X-Rays  
10<sup>4</sup> Independent Perfect Crystals

Note: For resolution  $>300$  meV, bending can be OK.

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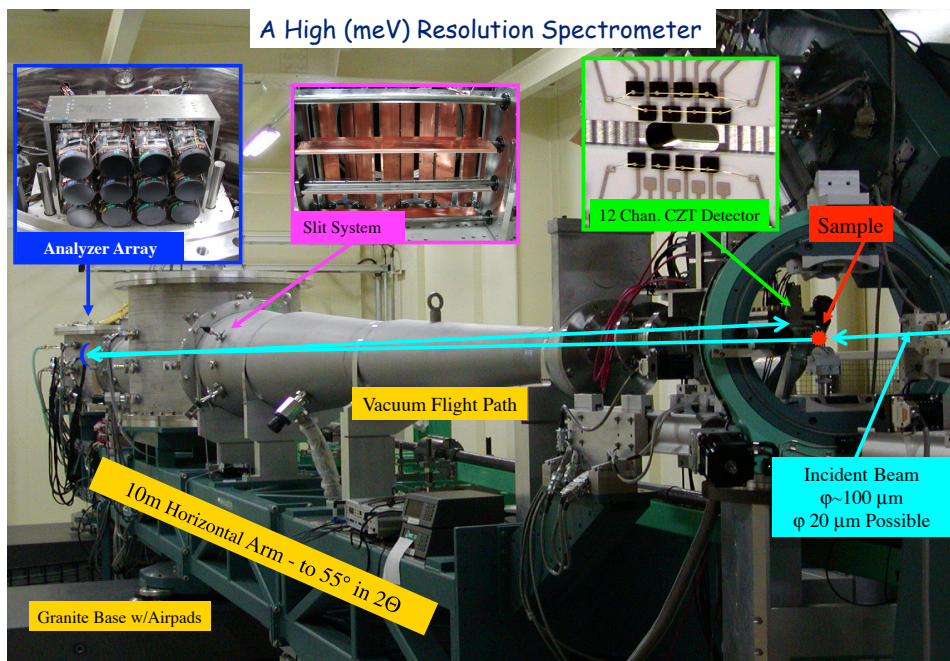
## Analyzer Crystal



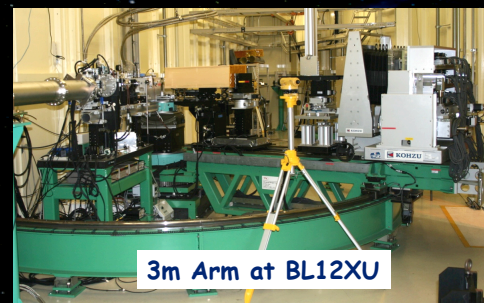
9.8 m Radius, 10cm Diameter  
50 or 60  $\mu\text{m}$  blade, 2.9 mm depth, 0.74 mm pitch  
Channel width (after etch):  $\sim 0.15$  mm  
60 to 65% Active Area

Not so easy...

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## A Medium Resolution Spectrometer



Medium Resolution Spectrometer:  
Arm Radius: 1 to 3 m  
Resolution:  $\sim 0.1$  to 1-eV  
Used for RIXS and NRIXS

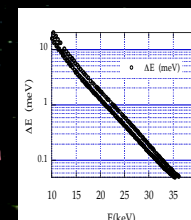
BL12XU BL11XU BL43LXU

Shorter Possible  
(later, if time)

Note difference between RIXS and NRIXS

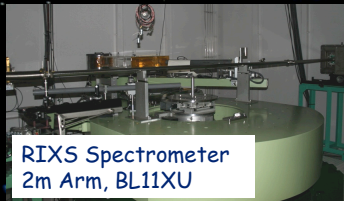
NRIXS: Choose the energy to match the optics

RIXS: Resonance chooses energy  $\rightarrow$  usually worse resolution

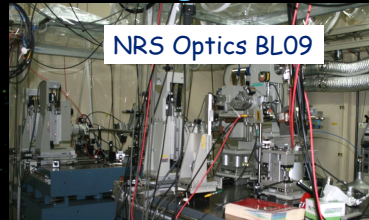


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## Other Spectrometers @ SPRING-8



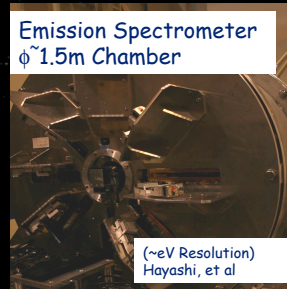
RIXS Spectrometer  
2m Arm, BL11XU



NRS Optics BL09



Compton Spectrometer BL08



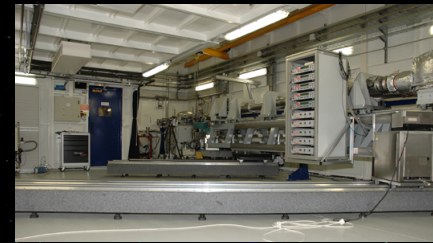
Emission Spectrometer  
 $\phi \sim 1.5\text{m}$  Chamber

(~eV Resolution)  
Hayashi, et al

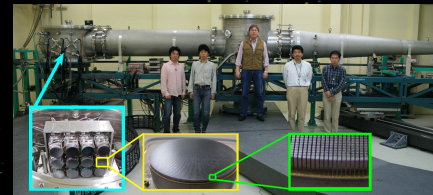
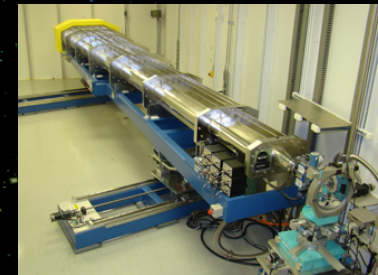
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## High Resolution Spectrometers

ESRF (ID28)



APS (Sector 30)



SPRING-8 BL35XU

HRXS  
~10m scale instruments

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## Atomic Dynamics: Systems and Questions

### Disordered Materials (Liquids & Glasses):

20+ years of IEXS → Nearly all good questions answered.

How do dynamical modes survive the cross-over from the long-wavelength continuum/hydrodynamic regime to atomic length scales?

### Crystalline Materials:

Basic phonon model does very well → Specific questions needed.

Phonon softening & Phase transitions (e.g. CDW Transition)

Thermal Properties: Thermoelectricity & Clathrates

Sound Velocity in Geological Conditions

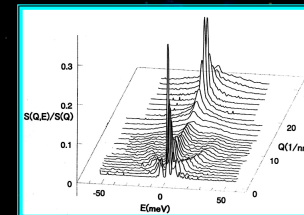
Pairing mechanism in superconductors

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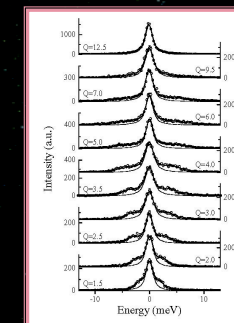
## Disordered Materials

Liquids & Glasses

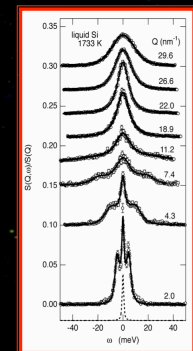
First Glance: Triplet response similar for most materials.  
Dispersing Longitudinal Sound Mode  
+ Quasi-Elastic peak



I-Mg (Kawakita et al)



a-Se (Scopigno et al)

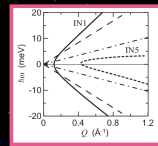


l-Si (Hosokawa, et al)

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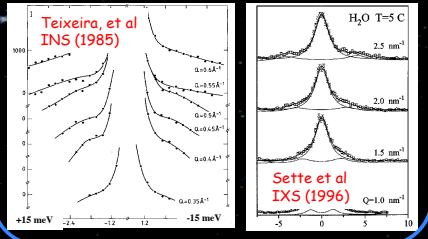
## The IXS Advantage

IXS has no kinematic limitations ( $\Delta E \ll E_i$ )  
Large energy transfer at small momentum transfer  
→ excellent access to mesoscopic length scales



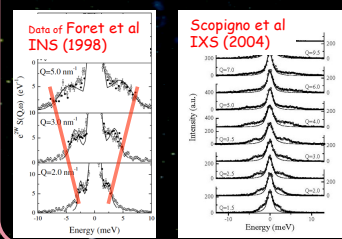
INS Diagram

### Water



Also: No Incoherent Background  
Small Beam Size ( $\phi < 0.1 \text{ mm}$ )

### Glassy-Se



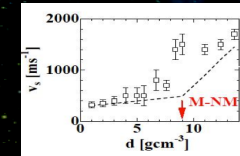
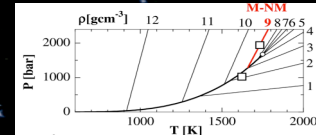
But:  $< 1 \text{ meV}$  resolution is hard  
Low Rates for Heavy Materials

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## "Fast Sound" at the Metal-Non-Metal Transition in Liquid Hg

Universal Phenomenon in Liquids:

Expand a liquid metal enough and it becomes an insulator.



Ultrasonic Velocity

Suggests a change in the microscopic density fluctuations...

Probably general phenomenon...  
but no confirmation yet.  
(Next M-I transition under discussion)

Ishikawa, Inui, et al, PRL 93 (2004) 97801

~2 months of beam time...

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## On Positive Dispersion

Very General feature:

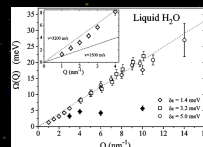
As  $Q$  increases the phase velocity of the acoustic mode becomes larger than the Low- $Q$  (e.g. ultrasonic) sound velocity.

Casual explanation

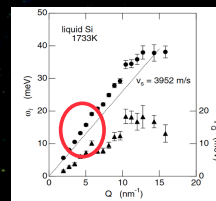
For smaller length scales (high  $Q$ ) and higher frequencies, a liquid, locally, resembles a solid which has a faster sound velocity.

Partial explanation in terms of a visco-elastic model...

Scopigno & Ruocco RMP 2005  
Ruocco & Sette CMP 2008  
Bryk et al JCP 2010



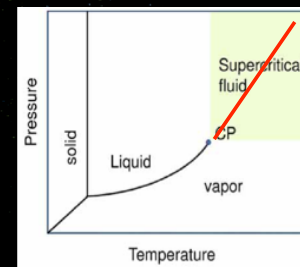
Sette et al



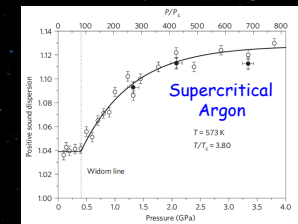
Hosokawa, et al

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## Dynamical Distinction



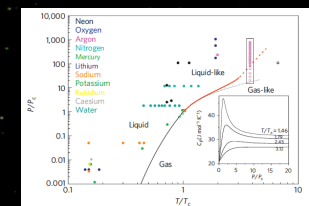
Widom Line  
Maximum in  $C_p$



Simeoni et al NPhys 2010

Take the presence of Positive Dispersion as the definition of liquid-like behavior

Gorelli et al, PRL (2006)  
Simeoni et al, NPhys (2010)  
Also Bencivenga et al EPL (2006)

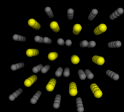
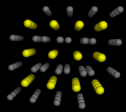


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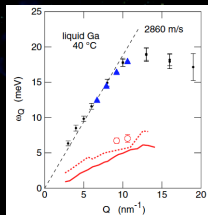
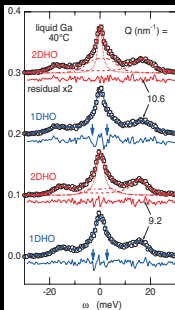
# Shear Mode in a Simple Liquid

Pressure Wave in a Liquid:  
Nearly Always Visible

Shear Wave -> Harder...

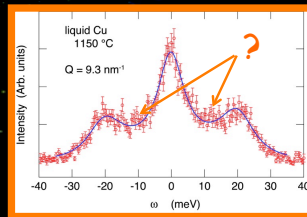


$$S(\mathbf{Q}, \omega) \approx \int dt e^{-i\omega t} \int d\mathbf{r} \int d\mathbf{r}' e^{i\mathbf{Q} \cdot (\mathbf{r} - \mathbf{r}')} \langle \rho(\mathbf{r}', t) \rho(\mathbf{r}, t = 0) \rangle$$



Weak, but significant, signal.

Hosokawa, et al, PRL (2009)



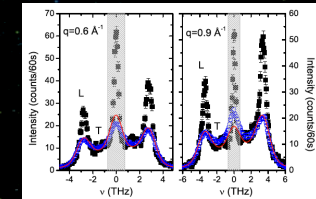
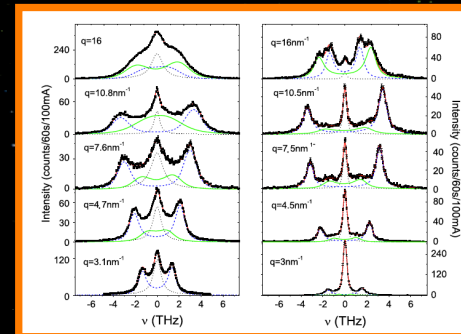
Next experiment: l-Cu  
2.5 Days -> ?

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# Liquid Excitations = Solid + Disorder?

Giordano & Monaco, PNAS (2010)

IXS from Na: Above & Below  $T_M$



Black = Polycrystalline Na  
Blue = Liquid Na

Red = Polycrystal + Scaling by  
Density, T, & Blurring...

Not bad ...

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# Phonons in a Crystal

Normal Modes of Atomic Motion = Basis set for small displacements

Must have enough modes so that each atom in a crystal can be moved in either x,y or z directions by a suitable superposition of modes.

If a crystal has N unit cells and R atoms/Cell then it has  
3NR Normal Modes

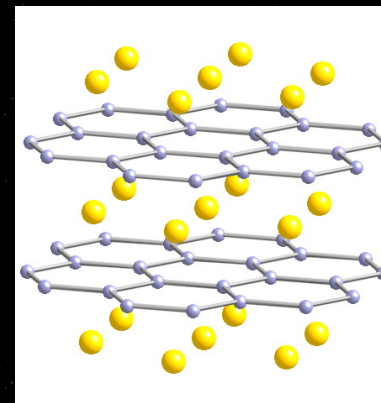
Generally: Consider the unit cell periodicity separately  
by introducing a "continuous" momentum variable,  $\mathbf{q}$ .

-> 3R modes for any given  $\mathbf{q}$

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# MgB<sub>2</sub> As An Example

Layered Material  
Hexagonal Structure



B Layer

Mg Layer

B-B Bond is Short  
& Stronger

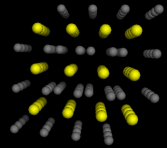
Mg-Mg Bond is  
Longer & Weaker

3 Atoms/cell -> 9 modes / Q Point

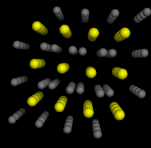
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## Acoustic and Optical Modes

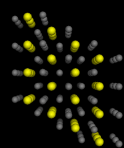
Acoustic Modes are Continuum (Smooth) Modes



LA Mode  
Compression Mode

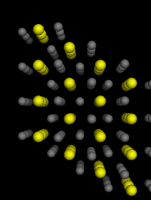


TA Mode  
Shear Mode

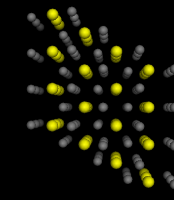


Optical Mode  
Atoms in one unit cell  
move against each-other

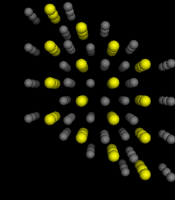
## Dispersion of an Optical Mode



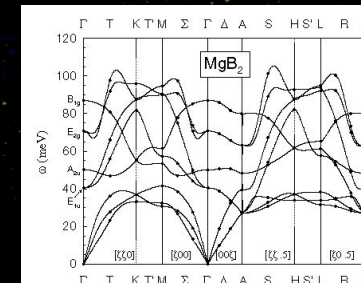
(0 0 0)



(0.25 0 0)



(0.5 0 0)



## Phonons in a Superconductor

Conventional superconductivity is driven by lattice motion.

"Phonon Mediated" - lattice "breathing" allows electron pairs to move without resistance.

Original Picture: **Limited** interest in *specific* phonons...

Now: Lots of interest as this makes a huge difference.  
Particular phonons can couple very strongly to the electronic system.

How does this coupling appear in the phonon spectra?

Softening: Screening lowers the energy of the mode  
(abrupt change  $\leftrightarrow$  Kohn Anomaly)

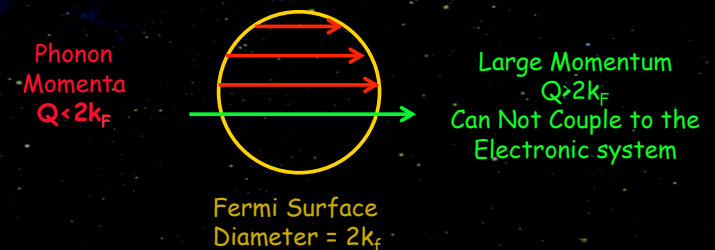
Broadening: Additional decay channel (phonon  $\rightarrow$  e-h pair)  
reduces the phonon lifetime

## Electron Phonon Coupling

& Kohn Anomalies

On the scale of electron energies, a phonon has nearly no energy.  
A phonon only has momentum.

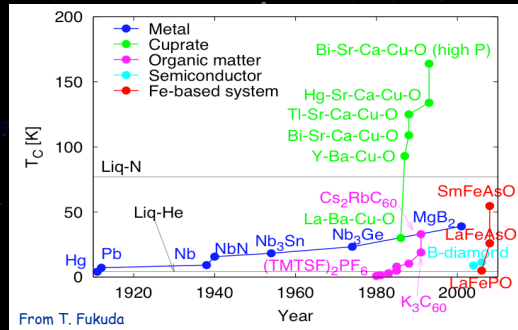
So a phonon can move electrons from one part of the Fermi surface to another, but NOT off the Fermi surface.



## Superconductors

Systems Investigated include

MgB<sub>2</sub>, Doped MgB<sub>2</sub>, CaAlSi, B-Doped Diamond  
 Hg1201, LSCO, YBCO, LESCO, Ti2212, BKBO, NCCO,  
 Bi2201, Bi2212, Nickelates, Oxchlorides  
 Fe-As Systems: LaFeAsO, PrFeAsO, BaKFeAs



Dark Blue Line: Conventional, Phonon-Mediated Superconductors

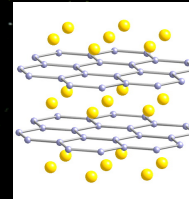
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## MgB<sub>2</sub>

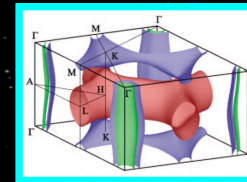
High T<sub>c</sub> (39K)

Nagamatsu, et al, Nature 410, (2001) 63.

Simple Structure...  
straightforward calculation.

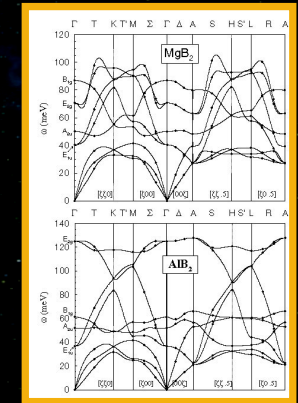


Electronic Structure



Kortus, et al, PRL 86 (2001)4656

Phonon Structure



Bohnen, et al, PRL, 86, (2001) 5771.

BCS (Eliashberg) superconductor with mode-specific electron-phonon coupling.

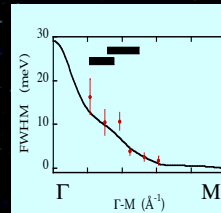
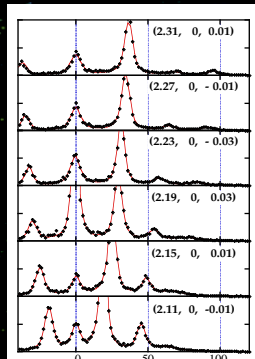
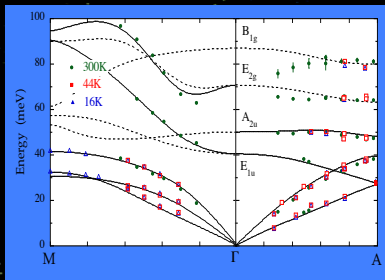
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## Electron-Phonon Coupling in MgB<sub>2</sub>

Dispersion

Spectra

Linewidth



Clear correlation between  
linewidth & softening.  
Excellent agreement with LDA Pseudopotential calculation.

PRL 92(2004) 197004: Baron, Uchiyama, Tanaka, ... Tajima

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## More Superconductors

Similar types of results for  
Mn Doped MgB<sub>2</sub>  
CaAlSi  
Boron Doped Diamond

Extrapolation to the High T<sub>c</sub> Copper Oxide Materials....

1. Much More Complex
2. Calculations Fail so interpretation is difficult

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## Phonons in the Cuprates...

Everyone has their favorite mode, or modes, usually focus on Cu-O planes

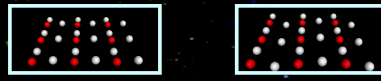
### In-Plane Mode:

Stretching mode



### Out of Plane Modes:

Buckling Mode



Apical Mode

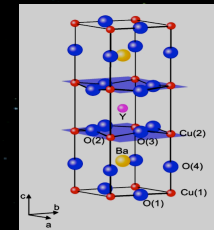


At the level of phonon spectra, the anomaly of the Bond Stretching Mode is very large

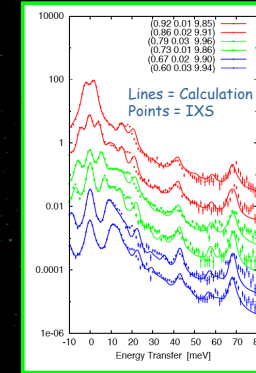
## Copper Oxide Superconductors Remain Challenging...

### De-Twinned YBCO: $\text{YBa}_2\text{Cu}_3\text{O}_{7-x}$

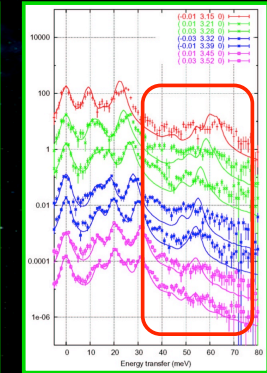
$T_c = 91 \text{ K}$



### C-axis modes



### In-Plane Modes



Beautiful Agreement

Problems

Shows Bond Stretching Anomaly Is Huge ( $\gg$  Buckling Anomaly)

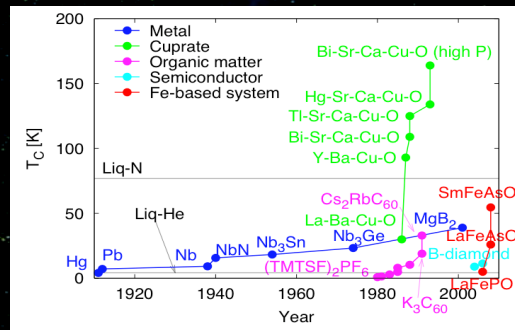
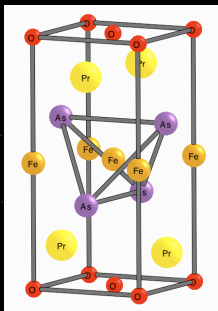
Compare IXS to Calculation

At low T ( $\sim 30 \text{ K}$ )

Bohnen, et al.

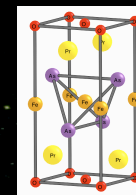
## Iron-Pnictide Superconductors

High- $T_c$  demonstrated February 2008 (Hosono's group)  
( $T_c$  saturated within months...)



Several families: Fe with Tetrahedral As (or Se)  
Proximity to Magnetic Order

## Phonons in the Iron Pnictides



1111 Materials  $\rightarrow$  8 Atoms/cell  
 $\rightarrow$  24 Modes (6 mostly oxygen)

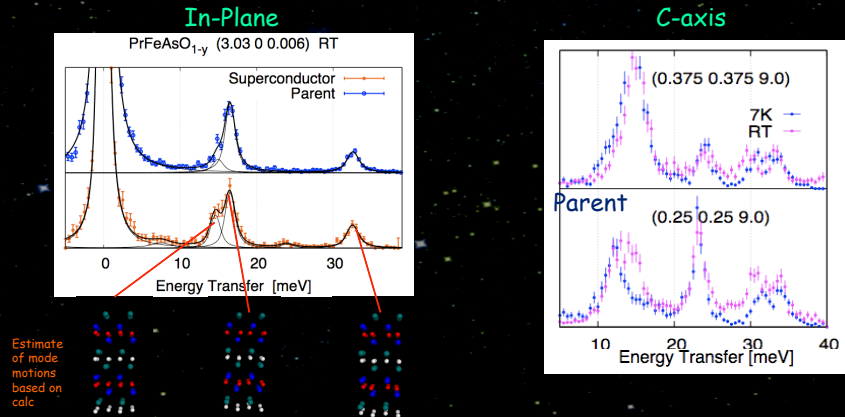
Magnetism  $\rightarrow$  16 Atoms / 48 Modes

No ab mirror plane  
 $\rightarrow$  Complex motions appear quickly as one moves away from gamma.

Phonon response, in itself, is remarkably plain:

- NO very large line-widths
- NO obvious anomalies
- NO asymmetric Raman lines

## Some Examples of Measured Spectra:



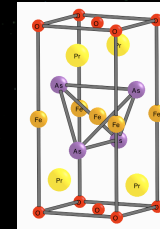
Clear differences in measured spectra (with doping, temperature)  
→ interpretations requires modeling...

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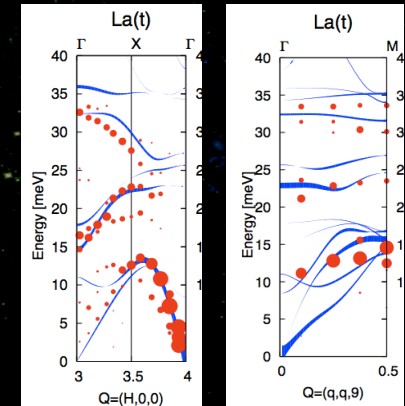
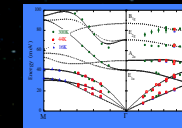
## Basic DFT (GGA) for PrFeAsO (No Magnetism)

Some agreement, but details are poor

Also, fails to get correct As height  
above the Fe planes.



Fe-As Bond Length  
Expt: 2.41 Å  
GGA: 2.31 - 2.33 Å



**A Better Model is Needed**

Symbol size: Measured Intensity  
Line Thickness: Calculated Intensity

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## Different Models:

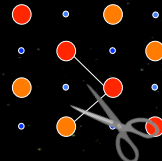
Original: Straight GGA for Tetragonal stoichiometric PrFeAsO

O<sub>7/8</sub>: Super cell 2x2x1 with one oxygen removed  
and softened Fe-As NN Force constant  
(31 atoms/prim cell, Tetragonal, No Magnetism)

Magnetic Orthorhombic: LSDA for LaFeAsO with  
stripe structure of De la Cruz (16 atoms/prim. cell, 72 Ibam)

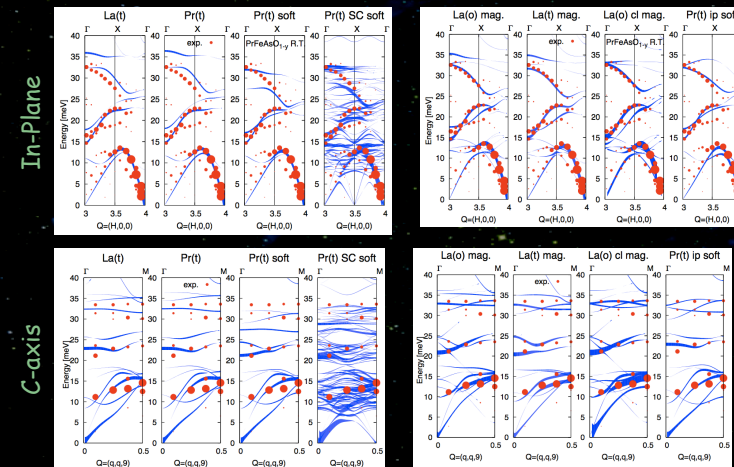
Magnetic Tetragonal: LSDA for LaFeAsO with stripes  
Force a=b (to distinguish effects of structure vs magnetism)

- ★ Soft: As "Original" but soften the FeAs NN Force constant by 30%
- ★ Clipped: Mag. Ortho. with cut force constant
- ★ Soft IP: "Original" but soften FeAs NN *In Plane* components



Original *ab-initio* Calculations: Nakamura & Machida  
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## Compare dispersion with various models



Red =  
Data (SC)

Blue =  
Calc.

Size:  
Intensity

Over all: Better fit with magnetic calculations  
And best fit with either "clipped" or "IP Soft" model

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Of the straight ab-initio calculations, magnetic models do better than non-magnetic due to softening of ferrmagnetically polarized modes  
However, they get details wrong, including too high an energy for AF polarized modes & predicting splitting that is not observed

Of the modified calculations, the in-plane soft generally seems best, but still data-calc difference are larger than doping/T effects.

Many people have suggested some sort of fluctuating magnetism, especially when magnetic calculations were seen to be better than non-magnetic calcs for the (non-magnetic) superconducting materials.

However, phonon response of parent and SC are nearly the same, and it seems unlikely that fluctuating magnetism is the answer in the parent material which shows static magnetism.

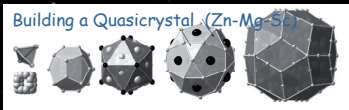
Still some missing ingredient(s) in the calculation  
-> Interpretation Difficult

Fitting of full spectra: intensity vs energy transfer.

Zeroth Approximation: All Samples are the Same  
Doping and Temperature Dependence are Weak

Differences between samples is generally much smaller than between any calculation and the data

-> Fit all spectra to a common model  
and then fit subsets of the data to determine effects of doping or phase transitions.

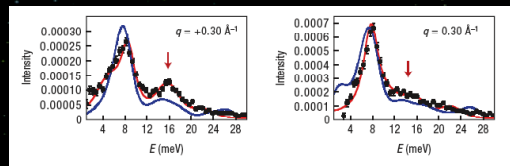
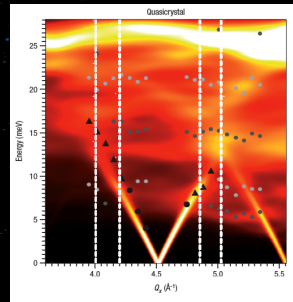


Periodic (BCC) -> Crystalline Approximant  
Aperiodic -> Quasicrystal

Compare to crystalline approximant & Simulation (2000 atoms/cell)

General Trend: Blurring out past a cutoff energy  
"Pseudo-Brillouin" zone size

De Boissieu, et al.  
Nature Materials, Dec 2007



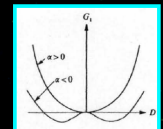
Red: Fits, Blue: Simulation

Develop spontaneous polarization over macroscopic (>~um) domains when T is below the ferroelectric transition temperature ( $T_0$ ). The origin is a displacement (off-centering) of ions. This is switchable by an external (electric) field.

Zeroth Approximation -> Two types of transitions

"Displacive" transition where there is a "continuous" below T  
"Soft Mode" transition Examples: BaTiO<sub>3</sub>, KTaO<sub>3</sub>, Gd(MoO<sub>4</sub>)<sub>3</sub>

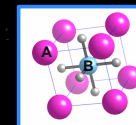
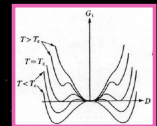
Soft Mode  
Nomenclature  
Ferrodistortive transition involves softening of gamma point mode (ferroelectric modes)  
Antiferrodistortive involves softening of zone boundary mode (unit cell size increases)



Lines & Glass

"Order-Disorder" transition where displacements occur first metastably and then condense. No soft mode.

Examples KH<sub>2</sub>PO<sub>4</sub>(KDP), NaNO<sub>2</sub>, Organics

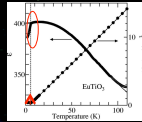
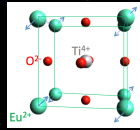


Perovskite structure (ABO<sub>3</sub>) popular as it is *relatively* simple and the cubic structure is inherently unstable.. Why?  
(3 atoms & one lattice constant)

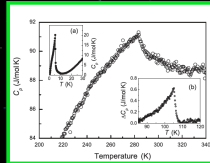
# Multiferroic $\text{EuTiO}_3$

Perovskite - Similar to  $\text{SrTiO}_3$

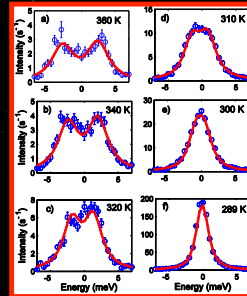
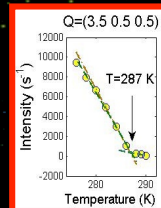
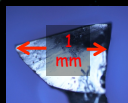
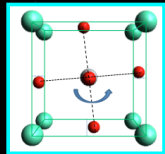
But with magnetism & coupling of magnetic & dielectric response



Katsufuji & Takagi, PRB, 2001

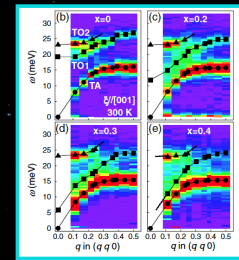
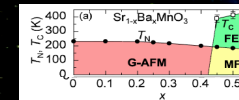
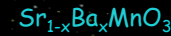


Phase transition just below RT - putative rotation oxygen octahedra. Calculations say disorder-order. Bussman-Holder, PRB, 2011



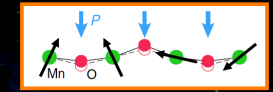
IXS  $\rightarrow$  Phonon Softening  $\rightarrow$  Displacive

# Other Multiferroicss

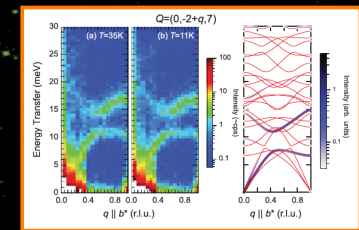


Classical ferroelectric soft mode

Sakai, et al. PRL 2011 (Tokura-lab)



Cycloidal spin structure coupled to development of polarization below 28K



No observed phonon softening may suggest a different (magnetic) driving force

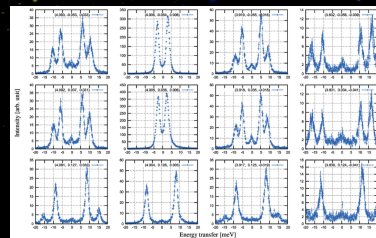
Kajimoto, et al. PRL 2009 (Tokura-lab)

# IXS under High Pressure

General Viewpoint: Just another thermodynamic variable.

Specific: elastic properties in extreme (geological) conditions based on IXS sound velocity measurements

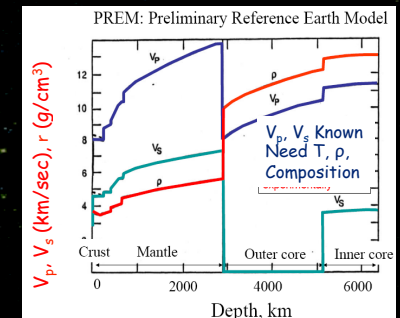
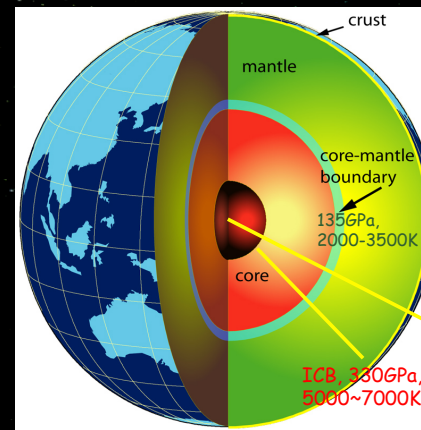
MgO Single Crystal in Ambient Conditions



Often: Just want the sound velocity  
Precision/Accuracy 0.2/0.8% using Christoffel's Eqn & 12 Analyzer Array  
H. Fukui, et al., JSR  
  
~1 Order Improvement in Precision Over Previous IXS

One Scan with 12-Analyzers

# High Pressure & Temperature for Geology



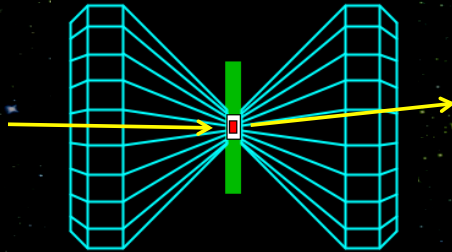
Earth's Center, 365 GPa  
6000~8000 K

Needed: Lab measurements relating T, Density & Composition to V

## Diamond Anvil Cells

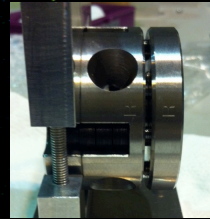
$P > 200 \text{ GPa}$   
 $T > 5000 \text{ K}$  (Laser Heating)

So far with IXS:  
 170 GPa or 3000K



Diamonds:  $2 \times 1.5 \text{ mm}$  Thk  
 Sample:  $\sim \Phi 20 \mu\text{m} \times 5 \mu\text{m}$  Thk  
 Also Gasket & Pressure Medium  
 P increases  $\rightarrow$  Smaller Sample & Gasket Hole

Small samples, Signal low, Poor signal to noise



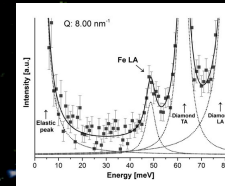
Std Cell  
Laser



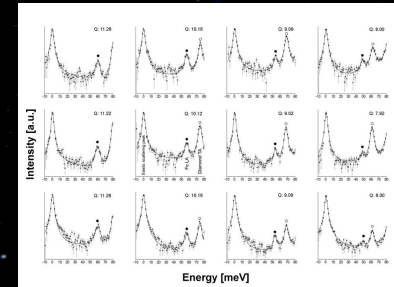
Cell with Internal Heating

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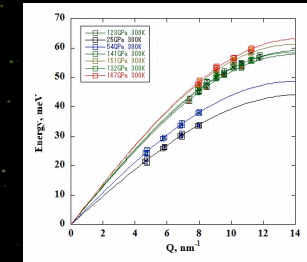
## IXS Data for Iron at 167 GPa



Very clear iron peak, but significant backgrounds  
 (Note diamond background can be tricky  
 $\rightarrow$  careful orientation is required)



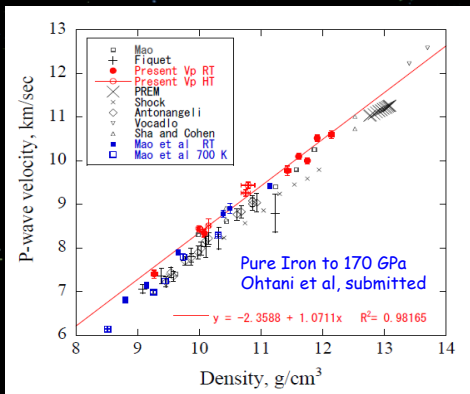
Sine fit gives velocity ( $V_p$ )



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## Sound Velocity in Pure Iron

Birch's Law: Linear relation between density and velocity.



SIMPLE, in principle

But 3 Facilities  $\rightarrow$   
 mostly different results

SP8 is faster than ESRF  
 and similar to APS  
 ESRF recently became  
 faster than before

T-Dependence:  
 APS is sensitive.  
 SP8 and ESRF are not.

WIP

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## Novel Uses of The Phonon Intensity

Phonon Cross Section:

$$\left( \frac{d^2\sigma}{d\Omega dE} \right)_{\mathbf{k}_1 \rightarrow \mathbf{k}_2} = \frac{k_2}{k_1} r_e^2 \left| \epsilon_1^* \cdot \epsilon_2 \right|^2 S(\mathbf{Q}, \omega)$$

$$S(\mathbf{Q}, \omega)_{1p} = N \sum_{1st \text{ Zone}} \sum_{3r \text{ Modes}} \sum_{Atoms} \left| \frac{f_d(\mathbf{Q})}{2M_d} e^{-W_d(\mathbf{Q})} \mathbf{Q} \cdot \mathbf{e}_{\mathbf{q}j} e^{i\mathbf{Q} \cdot \mathbf{r}_{jd}} \delta_{(\mathbf{Q}-\mathbf{q})_r} F_{\mathbf{q}}(\omega) \right|^2$$

$$F_{\mathbf{q}}^{Harmonic}(\omega) = \frac{1}{\omega_{\mathbf{q}j}} \left[ \langle n_{\omega_{\mathbf{q}j}} + 1 \rangle \delta(\omega - \omega_{\mathbf{q}j}) + \langle n_{\omega_{\mathbf{q}j}} \rangle \delta(\omega + \omega_{\mathbf{q}j}) \right]$$

In principle, the phonon polarization is complex, but in some cases; it can be simple, or smooth, letting one get information about  
 e.g. the form factor from frequency resolved measurements or sharp frequency changes from integrated measurements

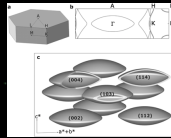
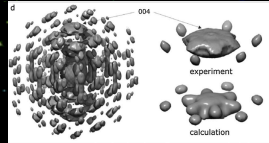
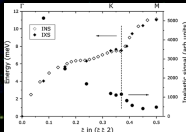
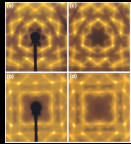
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# Using Thermal Diffuse Scattering (TDS)

Phonon Intensity  $\sim 1/w \rightarrow$  In simple materials can use intensity to gain insight about phonon frequencies

Long history... at least to Colella and Batterman PR 1970 (Va dispersion)

More sensitive  $\rightarrow$  See Kohn anomalies when phonons span the Fermi surface



Zn, Bosak et al, PRL 2009

TDS from Silicon

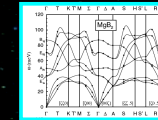
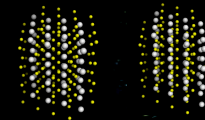
Holt, et al, PRL 1999

Detailed Phonon/FS behavior in SIMPLE materials  
More generally very useful, but not so detailed  
... use it to learn where to look...

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# Atomic $\rightarrow$ Electronic Dynamics

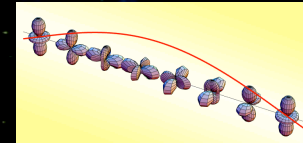
Atomic Dynamics



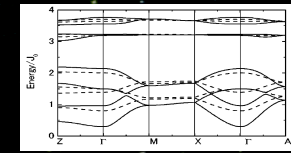
Correlated atomic motions (phonons) play a role in many phenomena (e.g. superconductivity, CDWs, phase transitions, thermoelectricity, magneto-elastic phenomena etc)

Electronic excitations similar: Orbitons...?

Orbiton Movie  
S. Maekawa



1 electron  $\rightarrow$  Very Weak



Calculated Orbiton Dispersion  
Ishihara

Key is to see momentum dependence (dispersion).

First Attempt via IXS: NJP 2004

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# d-d Excitations in NiO

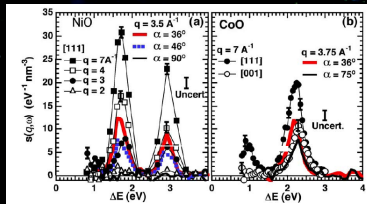
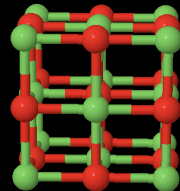
First something simple...

There exist well-defined excitations in the charge transfer gap of NiO  
Antiferromagnet ( $T_N$  523K), (111) Spin order

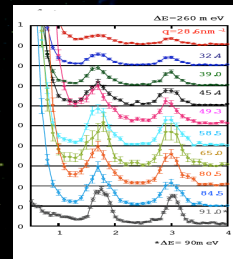
Long and Distinguished History

First (resonant) IXS experiments (Kao, et al)

Non-Resonant IXS,  $\Delta E \sim 300$  meV



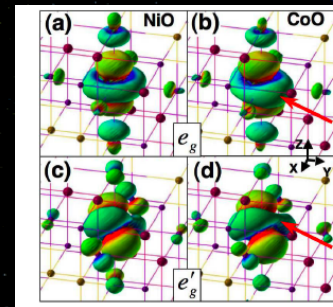
Larson, et al, PRL 99 (2007) 026401



Cai, et al, BL12XU, Unpublished

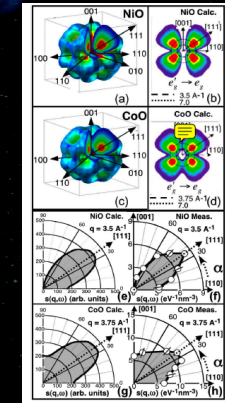
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# Orientation Dependence

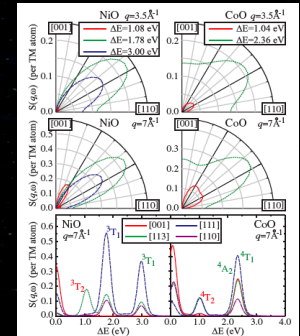


Orbitals

Results of Wannier function analysis of LDA+U calcs of Larson et al/PRL (2007)



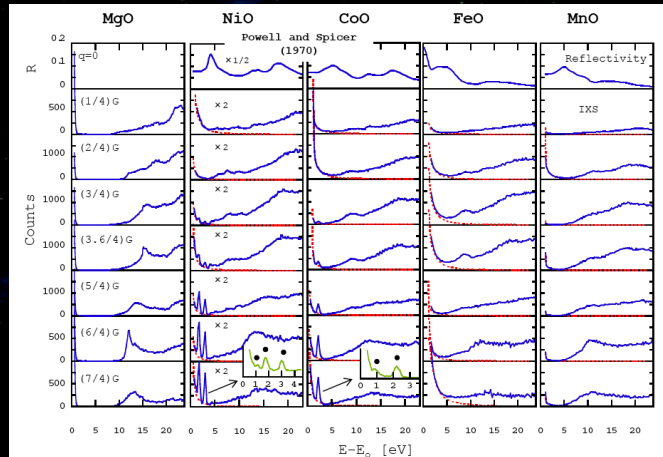
Scattered Intensity



Cluster calculations  
Haverkort, et al PRL (2007)

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## Larger Energy Range



Hiraoka et al

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## "Momentum Resolved Optical Spectroscopy"

**Conventional Optical Spectroscopy:**  
(Absorption, Reflectivity)

Information on electronic energy levels but *without* information on inter-atomic correlations or atomic structure

With x-rays, the short wavelength allows direct probe at atomic scale:

*Is an excitation collective or local (does it disperse)?*

*What is the atomic symmetry of an excitation?*

*How does it interact with the surrounding environment?*

Resonant experiment vs non-resonant IXS experiment.

Non-resonant experiment is simpler and can have higher resolution  
... but badly flux limited

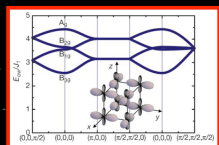
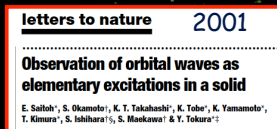
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## The Orbiton Story

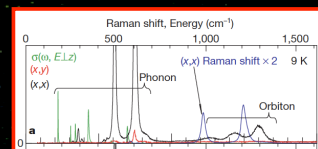
(One, mostly experimental, viewpoint)

Orbital order exists → there should be an equivalent excitation

Essential picture is of a correlated d-d excitation - change in electronic wave function on one atom is correlated with change at other atoms.



Calculated Dispersion



LaMnO<sub>3</sub>

But some dissent:

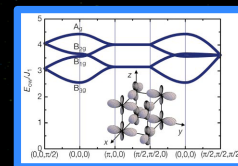
Two phonon peak?  
Gruning (n), Kruger (prl), Marin-Carron (prl)

And also corroboration

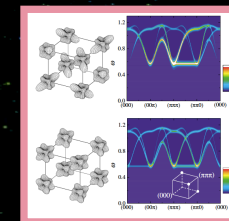
Raman spectra from different materials

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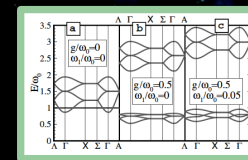
## Calculated Orbiton Dispersion



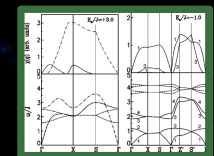
Saitoh et al, (N 2001)



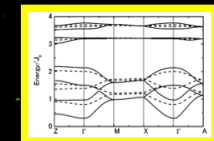
Khaliullin & Okamoto (PRL 2002)



van den Brink (PRL 2001)



Oles, Feiner, Zaanen (PRB 2000)



Ishihara (PRB 2004)

Still Some Debate:

Energy scale?

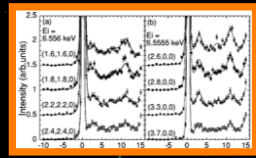
Coupling to phonons and/or spin?

Linewidth small or large?

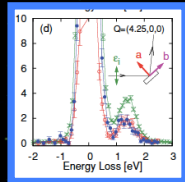
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# Resonant IXS (RIXS)

## K-Edge RIXS (d-d excitations)



LaMnO<sub>3</sub> Inami, et al (prb 2003)



KCuF<sub>3</sub> Ishii, et al (PRB 2011)

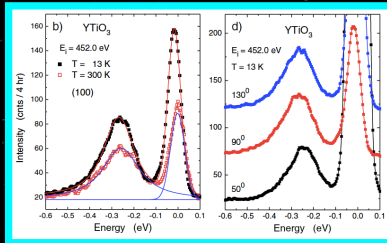
Resolution Improving:  
1000 → 250 meV → 70 meV

2011: STILL NO DISPERSING EXCITATIONS

## Soft x-ray RIXS (SRIXS)

Ulrich, Ament, et al (PRL 2009)  
At SLS/ADDRESS

L<sub>3</sub> in YTiO<sub>3</sub>, 55 meV Resolution at 450 eV



2-orbital signal at 250 meV...

# Recent Work

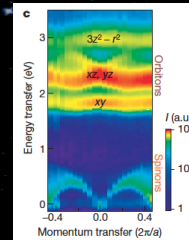
## LETTER

May, 2012

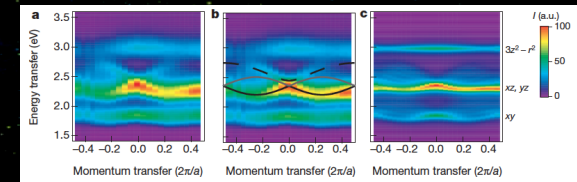
doi:10.1038/nature10974

## Spin-orbital separation in the quasi-one-dimensional Mott insulator Sr<sub>2</sub>CuO<sub>3</sub>

J. Schlappa<sup>1,2</sup>, K. Wohlfeld<sup>1</sup>, K. J. Zhou<sup>1</sup>, M. Mourigal<sup>1</sup>, M. W. Haverkort<sup>1</sup>, V. N. Strocov<sup>1</sup>, L. Hozoi<sup>1</sup>, C. Monney<sup>1</sup>, S. Nishimoto<sup>1</sup>, S. Singh<sup>1,2</sup>, A. Revcolevschi<sup>1</sup>, J.-S. Caux<sup>1</sup>, L. Patthey<sup>1,2</sup>, H. M. Rønnow<sup>1</sup>, J. van den Brink<sup>1</sup> & T. Schmitt<sup>1</sup>



## High Energy Excitation in Sr<sub>2</sub>CuO<sub>3</sub>



First attempt non-resonant (6 meV res) → No Signal

# Resonant IXS (RIXS/SIXS)

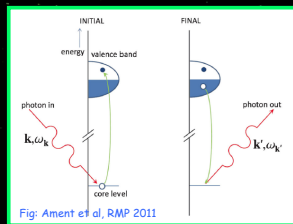


Fig: Ament et al, RMP 2011

## Direct RIXS

K Lines: Stronger, easier to reach for transition metals  
L Lines: Weaker, lower energy

Photons: Orbital angular momentum change,  $\Delta l=1$ , dominates:  $s \rightarrow p$  or  $p \rightarrow d$

Science: Most interest is in d-orbitals

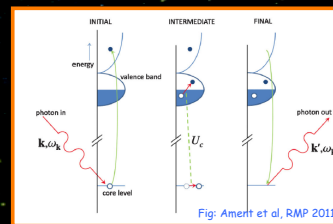


Fig: Ament et al, RMP 2011

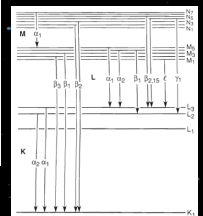
## Indirect RIXS

# Fluorescence Lines

Periodic Table of the Elements																	
Ground State Electron Configurations																	
1A	2A	3A	4A	5A	6A	7A	8A	1A	2A	3A	4A	5A	6A	7A	8A	1A	2A
1 H	2 He	3 Li	4 Be	5 B	6 C	7 N	8 O	9 F	10 Ne	11 Na	12 Mg	13 Al	14 Si	15 P	16 S	17 Cl	18 Ar
19 K	20 Ca	21 Sc	22 Ti	23 V	24 Cr	25 Mn	26 Fe	27 Co	28 Ni	29 Cu	30 Zn	31 Ga	32 Ge	33 As	34 Se	35 Br	36 Kr
37 Rb	38 Sr	39 Y	40 Zr	41 Nb	42 Mo	43 Tc	44 Ru	45 Rh	46 Pd	47 Ag	48 Cd	49 In	50 Sn	51 Sb	52 Te	53 I	54 Xe
55 Cs	56 Ba	57-71 Lanthanides	72 Hf	73 Ta	74 W	75 Re	76 Os	77 Ir	78 Pt	79 Au	80 Hg	81 Tl	82 Pb	83 Bi	84 Po	85 At	86 Rn
87 Fr	88 Ra	89-103 Actinides	104 Rf	105 Db	106 Sg	107 Bh	108 Hs	109 Mt	110 Ds	111 Rg	112 Cn	113 Nh	114 Fl	115 Mc	116 Lv	117 Ts	118 Og
89-103 Actinides	104 Rf	105 Db	106 Sg	107 Bh	108 Hs	109 Mt	110 Ds	111 Rg	112 Cn	113 Nh	114 Fl	115 Mc	116 Lv	117 Ts	118 Og	119 Uu	120 Uu
57 La	58 Ce	59 Pr	60 Nd	61 Pm	62 Sm	63 Eu	64 Gd	65 Tb	66 Dy	67 Ho	68 Er	69 Tm	70 Yb	71 Lu	72 Hf	73 Ta	74 W
89 Ac	90 Th	91 Pa	92 U	93 Np	94 Pu	95 Am	96 Cm	97 Bk	98 Cf	99 Es	100 Fm	101 Md	102 No	103 Lr	104 Rf	105 Db	106 Sg

\* values are based on theory and are not verified

Transition metals (Sc-Zn) → L = soft x-ray



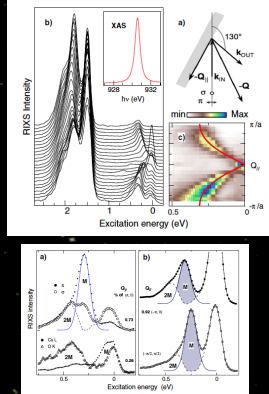
Ne: K 0.848  
Ar: K 2.96  
Kr: K 12.6 L 1.59  
Xe: K 29.8 L 4.1  
Rn: K 84.8 L 11.7

# Spin Waves Possible

PRL 105, 157006 (2010) PHYSICAL REVIEW LETTERS

Measurement of Magnetic Excitations in the Two-Dimensional Antiferromagnetic  $\text{Sr}_2\text{CuO}_2\text{Cl}_2$  Insulator Using Resonant X-Ray Scattering: Evidence for Extended Interactions

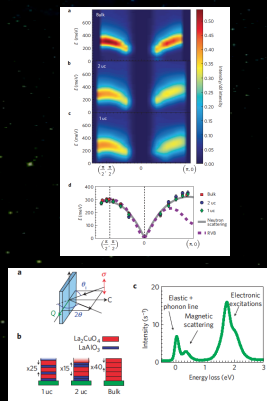
M. Giarice, B. Dalla Piazza, M. Moretti Sala, G. Chiarinelli, L. Braicovich, H. Berger, J. N. Hancock, D. van der Molen, T. Schmitt, N. N. Sirova, L. J. P. Ament, J. van den Brink, P.-H. Lin, P. Xu, H. M. Rønnow, and M. G. Cino



nature materials LETTERS

Spin excitations in a single  $\text{La}_2\text{CuO}_4$  layer

M. P. M. Dean, B. S. Springall, C. Momeny, K. J. Zhou, J. Persson, J. Bokor, B. Dalla Piazza, H. M. Rønnow, E. Morenzoni, J. van den Brink, T. Schmitt, and J. P. H. B. de Jongh



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# X-Ray Raman Scattering

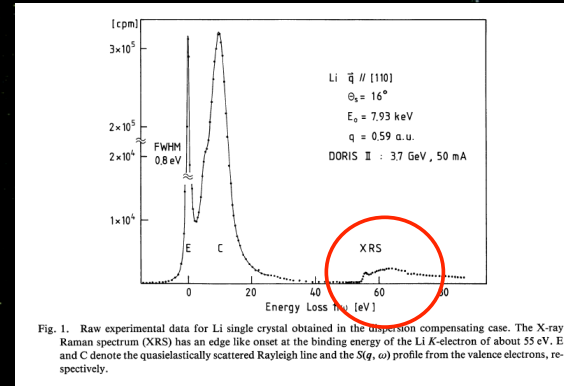


Fig. 1. Raw experimental data for Li single crystal obtained in the dispersion compensating case. The X-ray Raman spectrum (XRS) has an edge like onset at the binding energy of the Li  $K$ -electron of about 55 eV. E and C denote the quasielastically scattered Rayleigh line and the  $S(q, \omega)$  profile from the valence electrons, respectively.

Nagasawa, et al, J. Phys. Soc. Jpn. 58 (1989) pp. 710-717

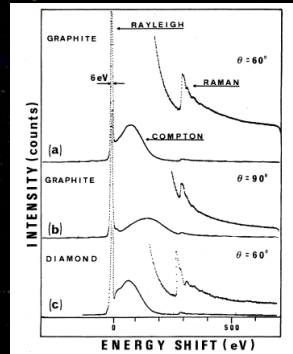


FIG. 2. (a) Inelastic-scattering spectrum from graphite observed at 60°. (b) Inelastic-scattering spectrum from graphite observed at 90°. (c) Inelastic-scattering spectrum from diamond observed at 60°. The Raman parts are inserted with an expanded scale. (a) and (b) were obtained with a Ge(440) dispersing crystal at 8900 eV excitation and (c) was obtained with a Ge(333) crystal at 8400 eV excitation. The Compton shift at 60° scattering does not coincide exactly for graphite and diamond because the excitation energy is slightly different.

Tohji&Udagawa, PRB 39 (1989) 7590

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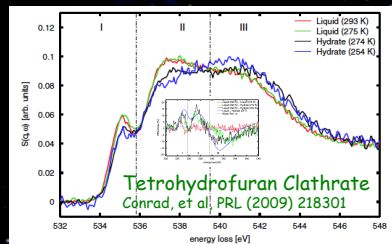
# X-Ray Raman Scattering

Suppose you would like to measure the structure of the oxygen k-edge (at 532 eV) of a sample inside of complex sample environment...

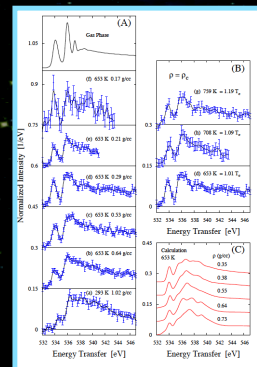
Diamond:

$l_{\text{abs}} < 0.5 \mu\text{m}$  500 eV  
 $l_{\text{abs}} \sim 2 \text{ mm}$  10 keV

Easier at 10 keV than 0.5 keV



Tetrohydrofuran Clathrate  
Conrad, et al PRL (2009) 218301



Supercritical Water

Ishikawa, et al,

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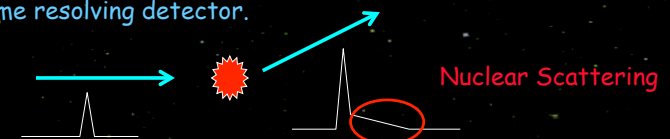
# Nuclear Inelastic Scattering

First-Demonstrated (Clearly) by Seto et al 1995

Mössbauer Resonances Exist in Different Nuclei...

Isotope	Transition energy (keV)	Lifetime (ns)	Alpha	Natural abundance (%)
$^{181}\text{Ta}$	6.21	8730	71	100
$^{169}\text{Tm}$	8.41	5.8	220	100
$^{83}\text{Kr}$	9.40	212	20	11.5
$^{57}\text{Fe}$	14.4	141	8.2	2.2
$^{151}\text{Eu}$	21.6	13.7	29	48
$^{149}\text{Sm}$	22.5	10.4	~ 12	14
$^{119}\text{Sn}$	23.9	25.6	~ 5.2	8.6
$^{161}\text{Dy}$	25.6	40	~ 2.5	19

Resonances have relatively long lifetimes so that if one has a pulsed source, one can separate the nuclear scattering by using a fast time resolving detector.

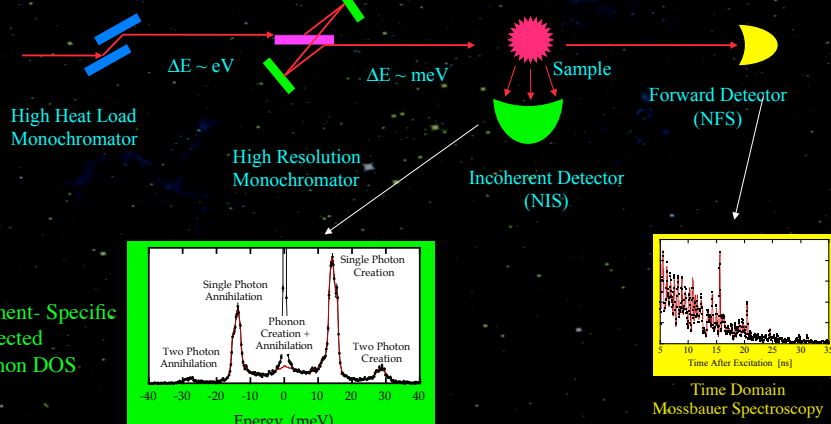


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## NIS Setup

Use a narrow bandwidth monochromator  
The nuclear resonance becomes the analyzer.

1.  $E_{in} = E_{res}$
2.  $E_{in} + E_{phonon} = E_{res}$
3.  $E_{in} - E_{phonon} = E_{res}$



Element-Specific  
Projected  
Phonon DOS

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## NIS: Good and Bad

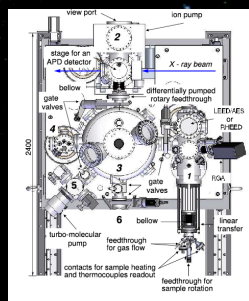
Important things to note:

1. Element and isotope selective.
2. Gives Projected Density of states NOT Dispersion (But it does this nearly perfectly)
3. Resolution given only by monochromator (analyzer is  $\sim eV$ )  
Easier optics but setup not optimized (compensated by large cross section)

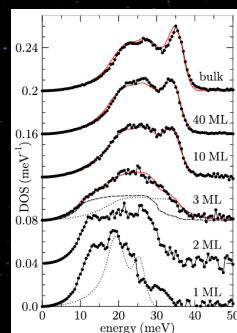
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## Surfaces by NIS

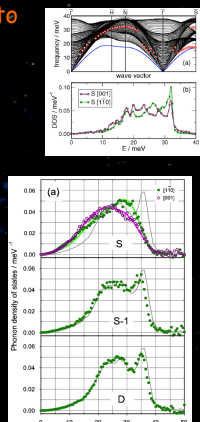
The large nuclear cross section allows sensitivity even to monolayers with relatively low backgrounds



In-Situ Deposition  
@ ESRF  
Stankov et al, JP 2010



$^{57}Fe$  on W(110)  
Stankov et al PRL (2007)



$^{57}Fe$  with  $^{56}Fe$   
Slezak et al PRL 2007

Also: Multilayers - Cuenya et al, PRB 2008

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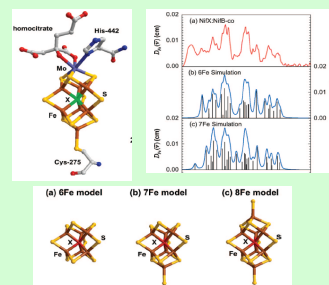
## Example (NRVS/NIS/NRIXS) In Biology

S. Cramer, et al, JACS

Measurement to determine the products of biological reactions via *site-selective* vibrational spectroscopy and comparison against calcs and model compound

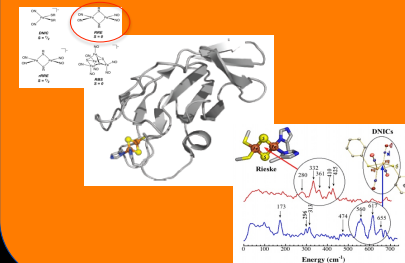
A compound in the nitrogen cycle...

Is X present? How many irons?



Toxicity of Nitric Oxide (NO)

-> Reaction products previously believed to be mononuclear are dinuclear



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## Compton Scattering

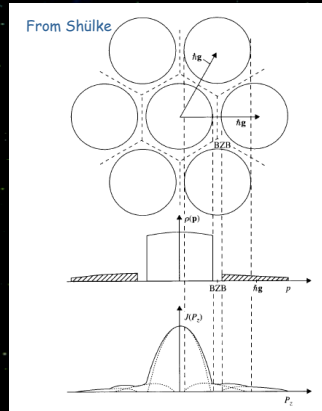
For very large  $Q$  and  $\Delta E \ll E$  one can take

$$S(\mathbf{Q}, \omega) = \frac{m}{\hbar Q} \iint dp_x dp_y \rho(p_z = p_0) \\ \equiv \frac{m}{\hbar Q} J(p_0)$$

Typical:  $Q \sim 100 \text{ \AA}^{-1}$   
 $E > 100 \text{ keV}$

I.e: Compton scattering projects out the electron momentum density.

Typical of incoherent scattering...



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## Three-Dimensional Momentum Density Reconstruction

Three-dimensional momentum density,  $n(\mathbf{p})$ , can be reconstructed from  $\sim 10$  Compton profiles.

$$J(p_z) = \iint n(\mathbf{p}) dp_x dp_y$$

Reconstruction:

- Direct Fourier Method
- Fourier-Bessel Method
- Cormack Method
- Maximum Entropy Method

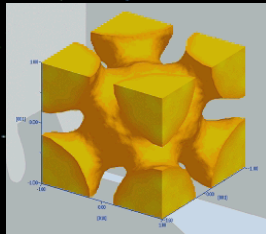
Momentum density,  $n(\mathbf{p})$

Note: a bulk probe that is tolerant of sample imperfections.

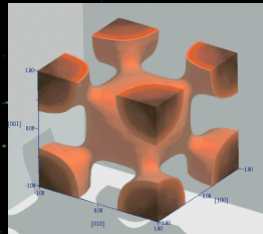
From Y. Sakurai

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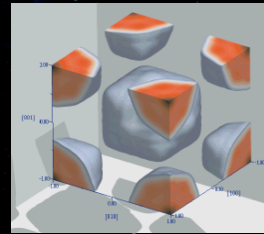
## Fermi surfaces of Cu and Cu alloys



Cu-15.8at%Al



Cu



Cu-27.5at%Pd

Determined by Compton scattering at KEK-AR

J. Kwiatkowska *et al.*, Phys. Rev. B 70, 075106 (2005)

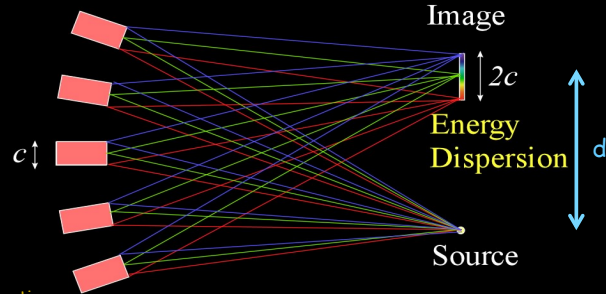
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# Reducing the Two-Theta Arm Size

Dispersion Compensation: Houtari, et al JSR (2005)

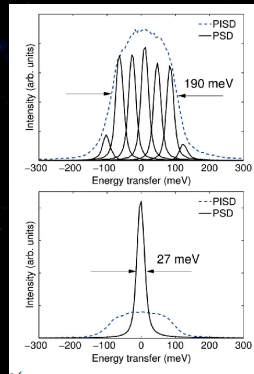
Crystal Cube Array



Animation  
D. Ishikawa

$$d = \frac{4R^2}{p} \frac{\Delta E}{E}$$

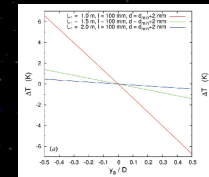
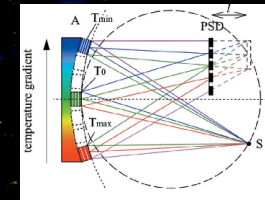
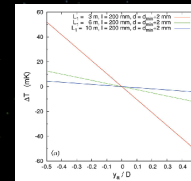
5 meV at 16 keV  
R=2m, p=0.1 → d=50 mm



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# Temperature Gradient Analyzer

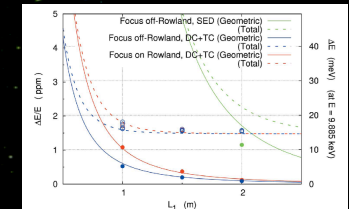
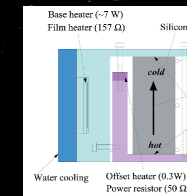
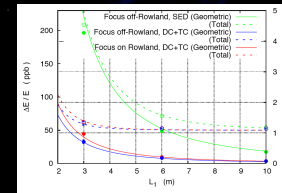
(Ishikawa & Baron, JSR 2010)



Longer Arm: DT~0.1C

l=150 to 200mm

Short Arm: DT: 1 to 10C



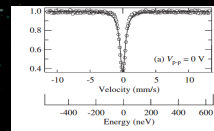
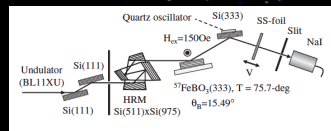
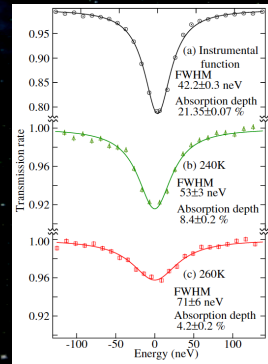
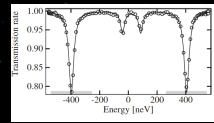
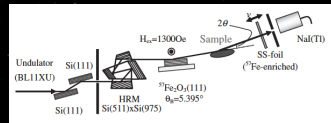
~ meV resolution at 3m

~5 meV at 1m

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# A Nano-Volt Spectrometer

Rayleigh Scattering of Synchrotron Mossbauer Radiation (RSSMR)



Masuda, Mitsui, Seto, et al, JJAP (2008, 2009)

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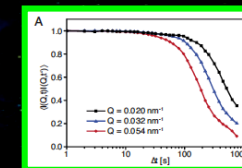
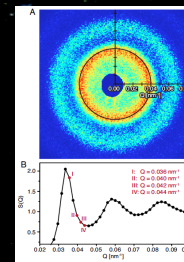
# Beyond Plane Waves

Usual Measurement is a two-point correlation function:

$$S(\mathbf{Q}, \omega) = \frac{1}{2\pi\hbar} \int dt e^{-i\omega t} \int d\mathbf{r} \int d\mathbf{r}' x e^{i\mathbf{Q} \cdot (\mathbf{r} - \mathbf{r}')} \langle \rho(\mathbf{r}', t) \rho(\mathbf{r}, t=0) \rangle$$

Complete picture includes higher order correlation functions

$$I(\mathbf{Q}, t) I(\mathbf{Q}', t') \propto \langle \rho(\mathbf{r}', t) \rho(\mathbf{r}, 0) \rho(\mathbf{s}', t') \rho(\mathbf{s}, 0) \rangle$$

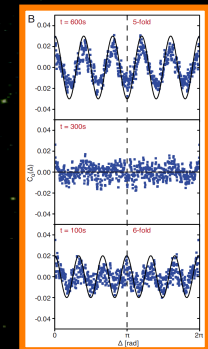


(A) Autocorrelation at One Q

(B) Cross-Correlation, Different Q

Wochner et al, PNAS (2009)

$$C_Q(\Delta) = \frac{\langle I(\mathbf{Q}, \varphi) I(\mathbf{Q}, \varphi + \Delta) \rangle - \langle I(\mathbf{Q}, \varphi) \rangle^2}{\langle I(\mathbf{Q}, \varphi) \rangle^2}$$

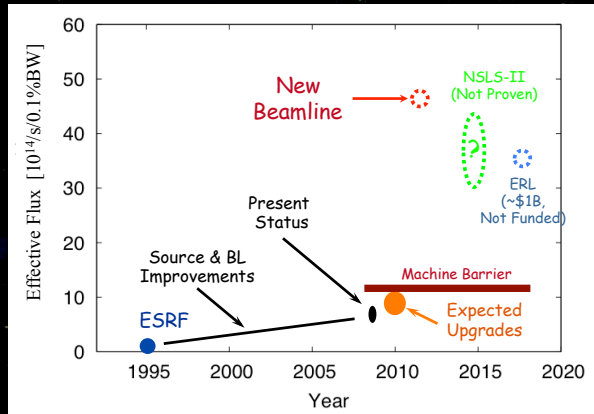


Ps Scales  
XFEL  
Or  
XFEL

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# IXS Beamline Evolution

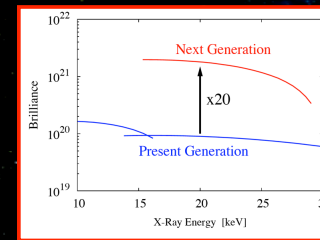
For meV Resolution at 20 keV



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# A Next Generation Beamline

Dramatic Improvement to Source and Spectrometer allows new science...



New Field: Electronic excitations

Also many expts now flux limited:  
Phonons in complex materials  
Extreme environments (HT, HP liquids)  
High pressure DAC work (Geology)  
Excitations in metal glasses  
Super-cooled liquids  
etc

## Improvements

Flux On Sample: x10  
Parallelization: x3  
Small Spot Size: x5



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# Quantum NanoDynamics Beamline (BL43LXU)

High resolution spectrometer: <1 to 6 meV  
10 m Arm, Good Q Resolution, to 12 Å<sup>-1</sup>  
Large (42 element) analyzer array.

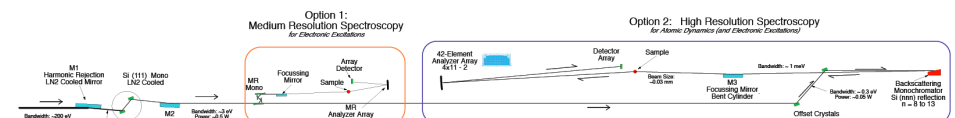
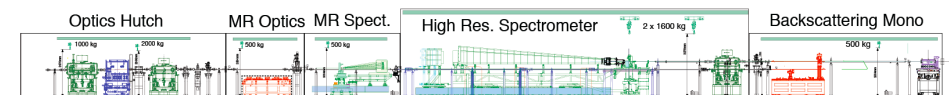
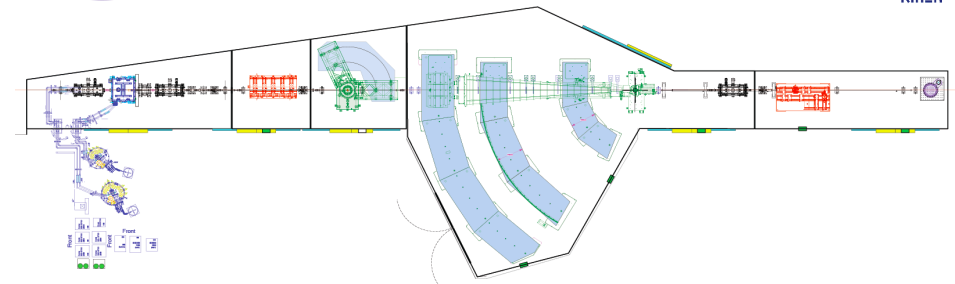
Medium resolution: 10-100 meV  
2m Arm; Large Q Acceptance  
Good tails using (888)

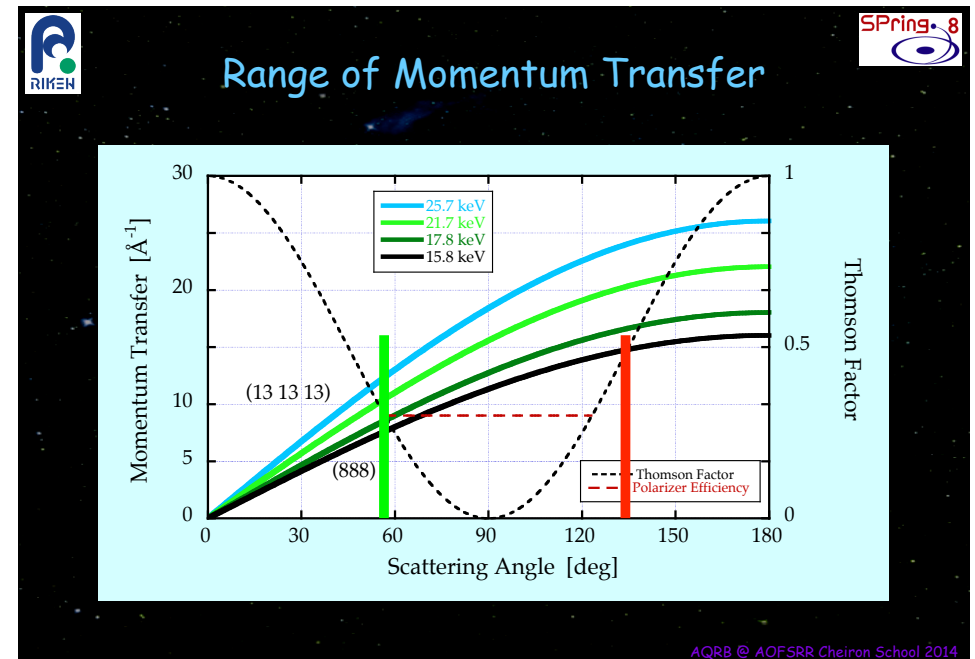
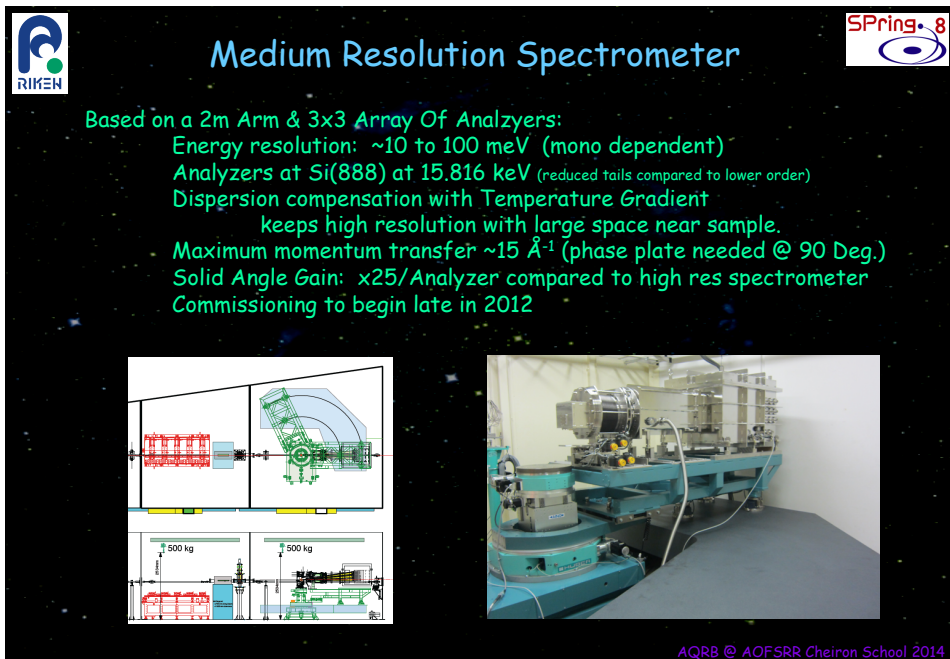
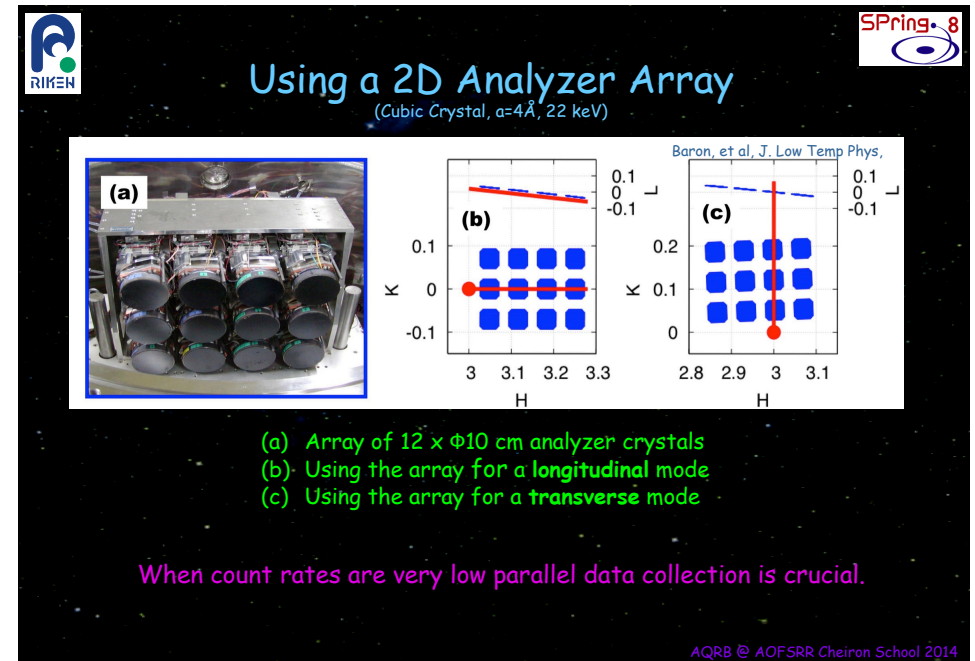


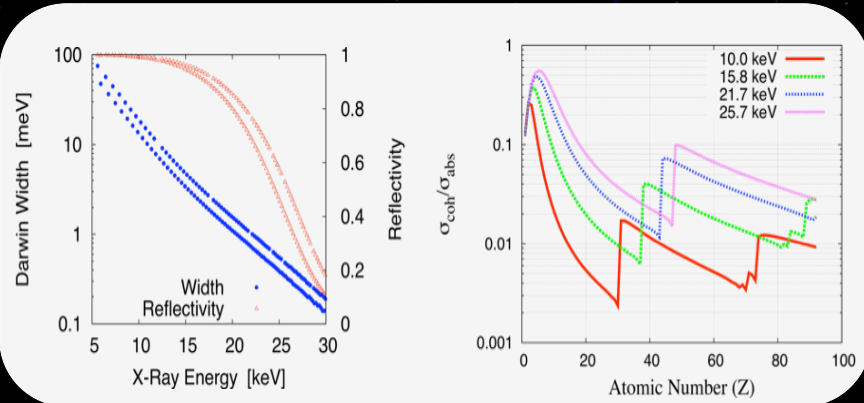
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# BL43LXU: RIKEN Quantum NanoDynamics (RQD) Beamline

for High-Resolution Non-Resonant Inelastic X-Ray Scattering  
A.Q.R. Barros, <http://www.spring8.or.jp/publications/p1338>



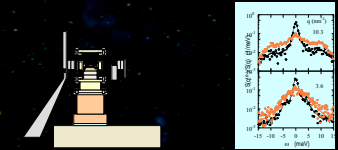
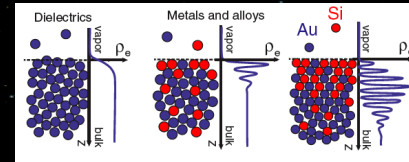




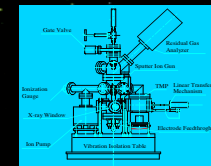
# Liquid Surfaces

Surface Dynamics are different than bulk...  
Surface Sensitivity (~5nm) is possible at Extreme Grazing Incidence

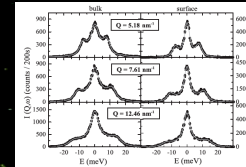
e.g. Surface Layering... (fig. Spyro, et al)



Favorable Tests in Air...  
UHV Chamber now in Progress  
(D. Ishikawa)



## Liquid Indium (ESRF)



Reichert, et al, PRL 2007

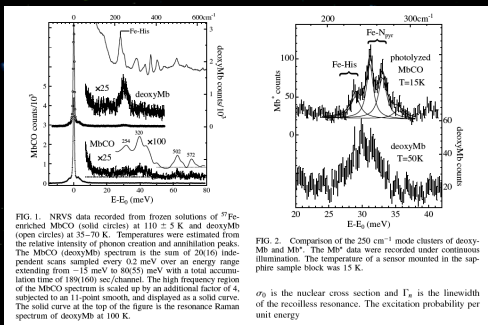
## NIS Example: Biological Macro-Molecules

VOLUME 86, NUMBER 21 PHYSICAL REVIEW LETTERS 21 MAY 2001

**Long-Range Reactive Dynamics in Myoglobin**

J. Timothy Sage,<sup>1</sup> \* Stephen M. Durbin,<sup>2</sup> Wolfgang Sturhahn,<sup>3</sup> David C. Wharton,<sup>1</sup> Paul M. Champion,<sup>1</sup> Philip Hession,<sup>2,3</sup> John Sutter,<sup>2,3</sup> and E. Ercan Alp<sup>3</sup>

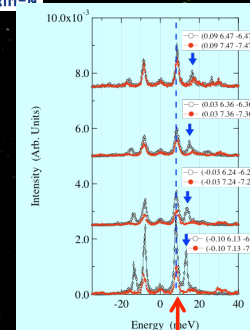
e.g.



Where element specificity can help a lot.

## SmRu<sub>4</sub>P<sub>12</sub>

S. Tsutsui, et al.  
JPSJ 77 (2008) 033601

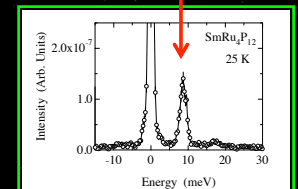
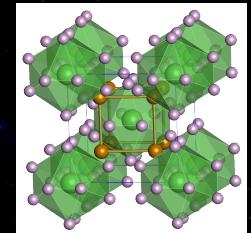


"Localized" Rattling Mode

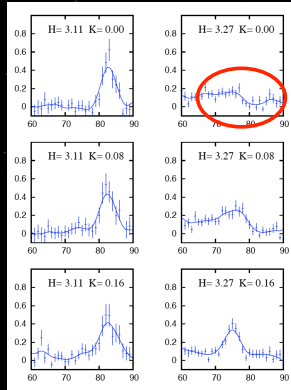
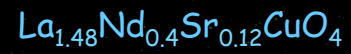
## Localized Nature Confirmed by IXS

(No Frequency Dispersion, Weak Intensity Dispersion, BUT Note Anticrossing!)

Sm Mode confirmed by (Sm specific) Nuclear Inelastic Scattering



Anti-Crossing Subsequently Confirmed  
Christensen et al, Nature Materials



D. Reznik, et al

2.5 days

Phonon anomaly (blurring) is highly localized in momentum space...

Expt done by a neutron scatterer because he could not get good enough resolution using neutrons

Forces a reinterpretation of some Neutron data (Reznik, Nature, 2006)

Note: IXS Q Resolution  
Analyzer array  
Count rate limited.